# Algorithms for computing Maximally Redundant Trees for IP/LDP Fast-Reroute 

draft-enyedi-rtgwg-mrt-frr-algorithm-00

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## MRT

- Maximally Redundant Trees
- A pair of directed spanning trees
- The common root is reachable along both of them
- The two paths along the two trees are maximally disjoint



## Why do we need this draft?

- We need a pair of MRTs rooted at each node
- All the nodes should compute the same!
- We will need standardization for MRT computation (algorithm) or results of that computation.


# Principles 

## Partial order <br> ADAG

Blocks and GADAG

## Partial order

- Partial order of a set (e.g. set of nodes)
- A relation like a normal set
- Except: not all the elements can be compared
- For some $\mathbf{a}$ and $\mathbf{b}$ neither $\mathbf{a}<\mathbf{b}$ nor $\mathbf{a}>\mathbf{b}$
- Graph representation:
- Directed Acyclic Graph (DAG)

- $\min <a<b<f<c<e<\max$
- $a<d<e$


## Finding node-disjoint paths

- Suppose that
- We have a partial order of nodes
- Exactly one min and max
- Each node (except min and max) has a lower and greater neighbor
- Walk down and up
- Min and max are reached
- The two paths are node-disjoint!

- $\min <a<b<f<c<e<\max$
- $a<d<e$


## Two paths to the same node

- DAG is not enough
- Let min and max be the same node!
- Resulting graph is an Almost DAG (ADAG)
- There is a single node, the root, such that without the root it is a DAG

- mimt<a<b<fl<c<e<mocax
- $a<d<e$


## Redundant paths to the root

- Blue path:
- Nodes must increase
- Red path:
- Nodes must decrease
- Load sharing is possible



## Finding an ADAG (2-connected networks)

- Phase 1 - basic partial ADAG
- Find a partial ADAG for a cycle containing the root
- Use either direction
- Extend partial ADAG into all nodes



## Finding an ADAG (2-connected networks)

- Phase 2 - extending
- Find a path from one "ready" node to the another
- Nodes along the path must not be ready (except the endpoints)
- Add the path to the ADAG in a "proper" direction



## Adding not used links

- Some links may be out of the ADAG


BAOKe<f

## How can ordering be kept up?

- ADAG is almost a DAG
- Let root be now only the smallest one
- Now, it's a DAG, create a topological sort
- This is a total order
- Add extra links with respect to this

Add back links to root and we have an ADAG using all links.


## What if the network is not 2-connected?

- We need to split the graph into blocks
- Block:
- Maximally 2-connected subgraph
- Two connected nodes
- (Isolated node)
- Each block has its local-root
- That is the cut-vertex towards the root
- Compute an ADAG in all the blocks
- This is a Generalized ADAG


## Generalized ADAG



- Block1• ront, a_h_c.d.e, f
- BlockZ: a
- Blocku: g, i, i, j, K


## The algorithm

MRTs in a block<br>MRTs in the whole network

## How to Find MRTs

- If it is complex, then we break the problem down
- Transform network into its blocks
- Find ADAGs in each block
- Connect up the ADAGs to make a GADAG
- Add all the other links in - with the proper directionality
- From a GADAG, compute your next-hops to each destination
- First for those in the same block
- Destinations outside the block inherit their nexthops from a proxy in the block


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## MRTs in a single block

- As the computing router S : From the GADAG, can use SPF and reverse SPF to find next-hops to all destinations in the same block
- SPF gives nodes definitely greater
- rSPF gives nodes definitely lesser
- Remaining nodes are not ordered
- Then use some simple rules


## MRTs in a single block: source perspective

- Find greater and lesser nodes
- Rules

| 1. If $\mathbf{S}<\mathbf{D}-$ | increase to D |
| :--- | :--- |
| 2. If $\boldsymbol{S}>\boldsymbol{D}-$ | increase to root |
| 3. $N$ order - | decrease to root |
| 4. If D =root - | increase to root |
| 5. If $S=$ root | increase to $D$ |


decrease to root
decrease to D
increase to root
decrease to root
decrease to D

Routing table of node $\mathbf{c}(\mathbf{S}=\mathbf{c})$ :

| Dest <br> ( D ) | Rule <br> Used | Blue <br> Next-hop | Red <br> Next-hop |
| :---: | :---: | :---: | :---: |
| a | 2 | e | b |
| b | 2 | e | b |
| d | 3 | b | e |
| e | 1 | e | b |
| f | 2 | e | f |
| root | 4 | e | b |

## MRTs in a single block: destination perspective

- Find greater and lesser nodes
- Rules

1. If $\mathbf{S}<\mathbf{D} \quad-\quad$ increase to $\mathbf{D}$
2. If $\mathbf{S}>\mathbf{D} \quad$ increase to root
3. No order - decrease to root
4. If $d=$ root - increase to root
5. If $s=$ root - increase to $D$

|  |  | ease to ease to ase to r ease to ease to |  |
| :---: | :---: | :---: | :---: |
|  | tination: | node c | = c) |
| $\begin{aligned} & \mathrm{Src} \\ & (\mathrm{~S}) \end{aligned}$ | Rule Used | Blue Next-hop | Red <br> Next-hop |
| a | 1 | b | root |
| b | 1 | c | a |
| d | 2 | a | e |
| e | 3 | root | c |
| f | 2 | c | e |
| root | 1 | a | e |

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## Inter-block MRTs

Proxy node: the last vertex in the block to the destination (along any path)


## Example - destination is node C



- Block1: root, a, b, c, d, e
- Block2: e, f
- Block3: f, g, h, i, j


## Summary

- Algorithm
- Find GADAG
- ADAG in each block
- Add not used links
- Find next-hops along the MRTs
- Do an SPF and an rSPF to find ordered nodes
- Use rules to find NHs your block
- Find proxy nodes


## Thanks for the attention

