

A photograph of a city skyline at night, with numerous buildings illuminated and their lights reflecting on the water in the foreground. The sky is dark, and the water is calm, creating a clear reflection of the city lights.

# Expansion of Virtual-Oriented Infrastructure

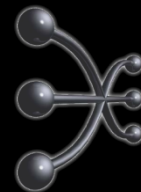
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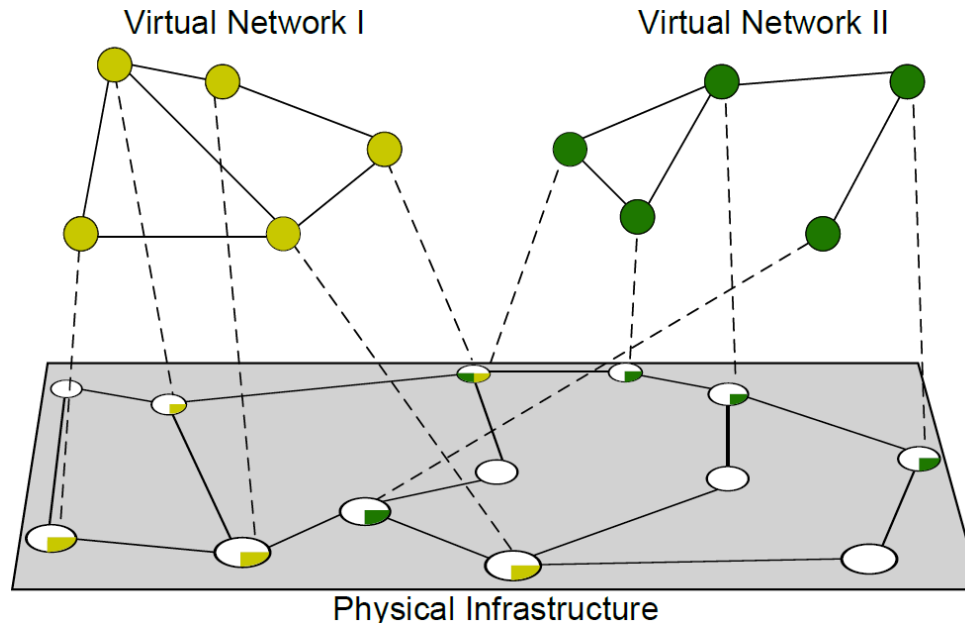
# Outline

- Introduction
- Related Work
- InP Network Expansion For Efficient VNE
- Evaluation
- Conclusion and Future Work

# Introduction

## Context

- **Network virtualization:** allows the coexistence of heterogeneous virtual networks sharing resources of the same physical infrastructure
- **Challenge:** efficient mapping of physical resources to virtual networks (Chowdhury et al. [2009], Houidi et al. [2011], Fajjari et al. [2011], Cheng et al. [2011], Cheng et al. [2012], Alkmim et al. [2013])



# Introduction

## Problem Definition and Motivation

- In previous work on Virtual Network Embedding, we observe:
  - **High rejection rates for VN requests** (up to 53%)
- We also verified (Luizelli et al. [2013]):
  - Subset of such rejection is caused by a temporary global outage of physical resources
  - An **expressive number** of rejection occurs in situation in which there are **sufficient resources available**

# Introduction

## Objective

- Propose a model for planning the expansion of InP networks
  - Reduce rejection rates
  - Increase resource consumption in the infrastructure
- By means of:
  - Formalization of an InP network expansion model in the context of network virtualization
  - Design of a heuristic approach to solve the model

# Related Work

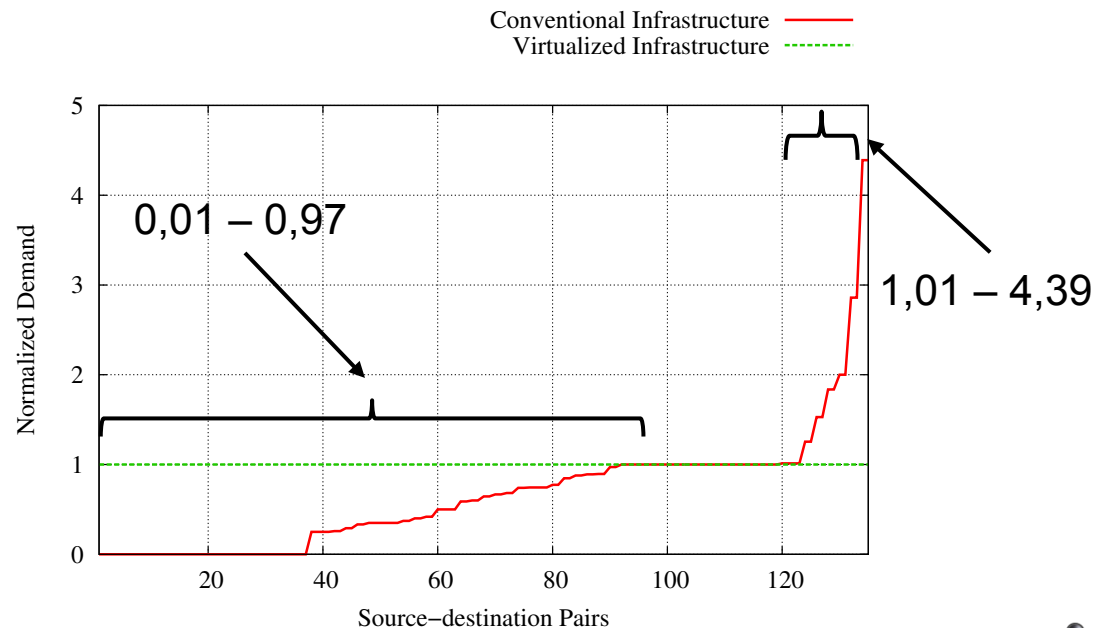
## Expansion/Planning Approaches

- Backbone network expansion:
  - Mukherjee et al. [1996], Ramaswami et al. [1996], Krishnaswamy et al. [2001], Curtis et al. [2009], Johnston et al. [2011]
- Data center network expansion:
  - Curtis al. [2012], Gao el al. [2012]
- All of them rely on the use of **demand matrices** to plan the expansions
- **We are not aware of previous attempts to investigate strategies for expanding the physical network of an infrastructure provider with the objective of enabling it to host a higher number of virtual networks**

# InP Network Expansion

## Why Are Demand Matrices not Suitable for Virtual Network-oriented Infrastructure Planning?

- Traditional expansion approaches based on demand matrices are not suitable for virtualized environments
- Virtualized InP exhibit comparatively more homogeneous resource distribution amongst physical devices



# InP Network Expansion: Overview

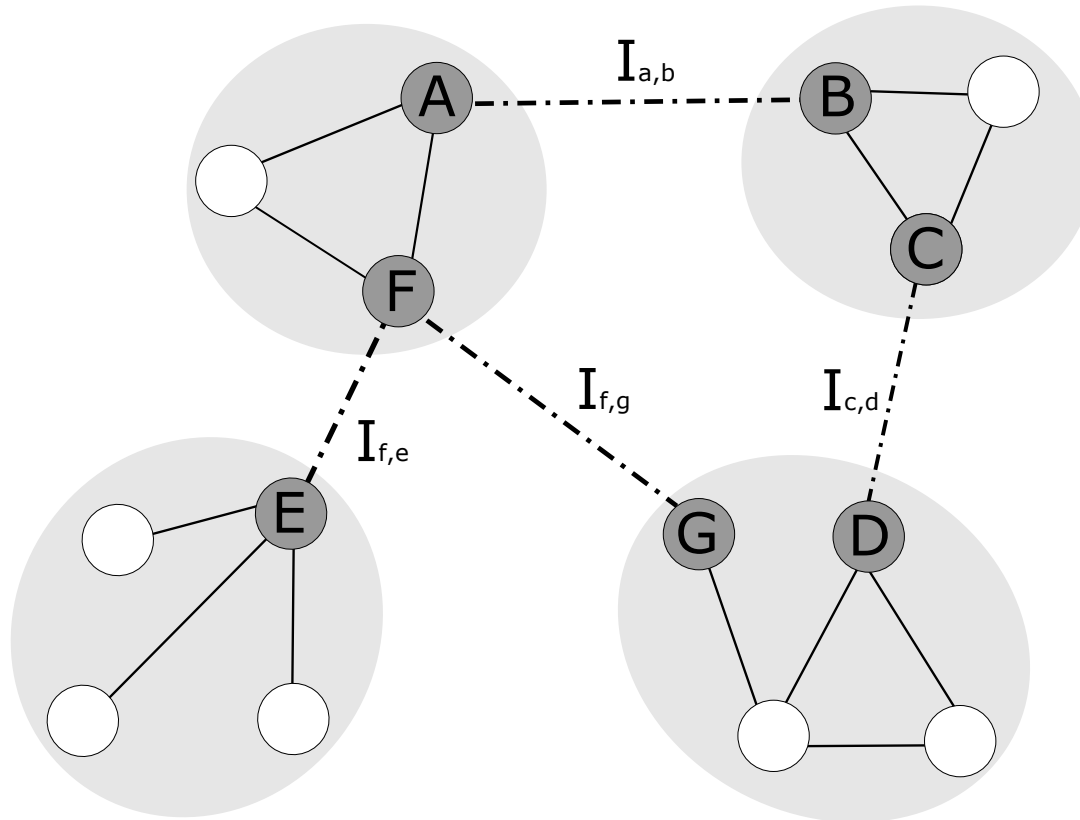
- One of the major causes of virtual network rejection in the context of VNE is the absence of a suitable partition
- As mentioned, InP networks have available resources
- The occurrence of partitions is directly correlated to the total exhaustion of available resource in specific devices (e.g., hubs and bridges)

**The above findings were the motivation for modeling the InP expansion problem**



# InP Network Expansion: Overview

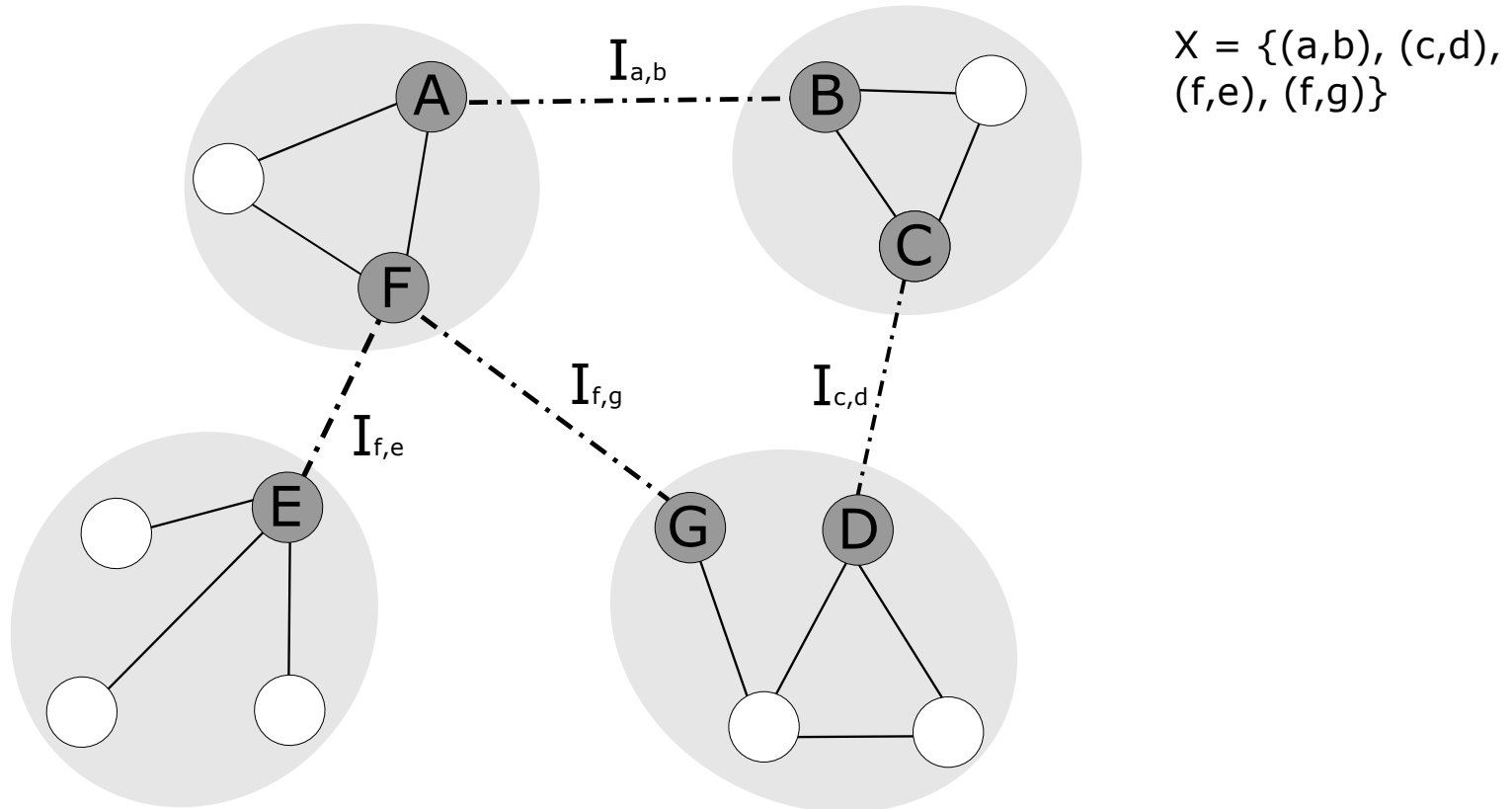
## Example



$X = \{(a,b), (c,d), (f,e), (f,g)\}$

# InP Network Expansion: Overview

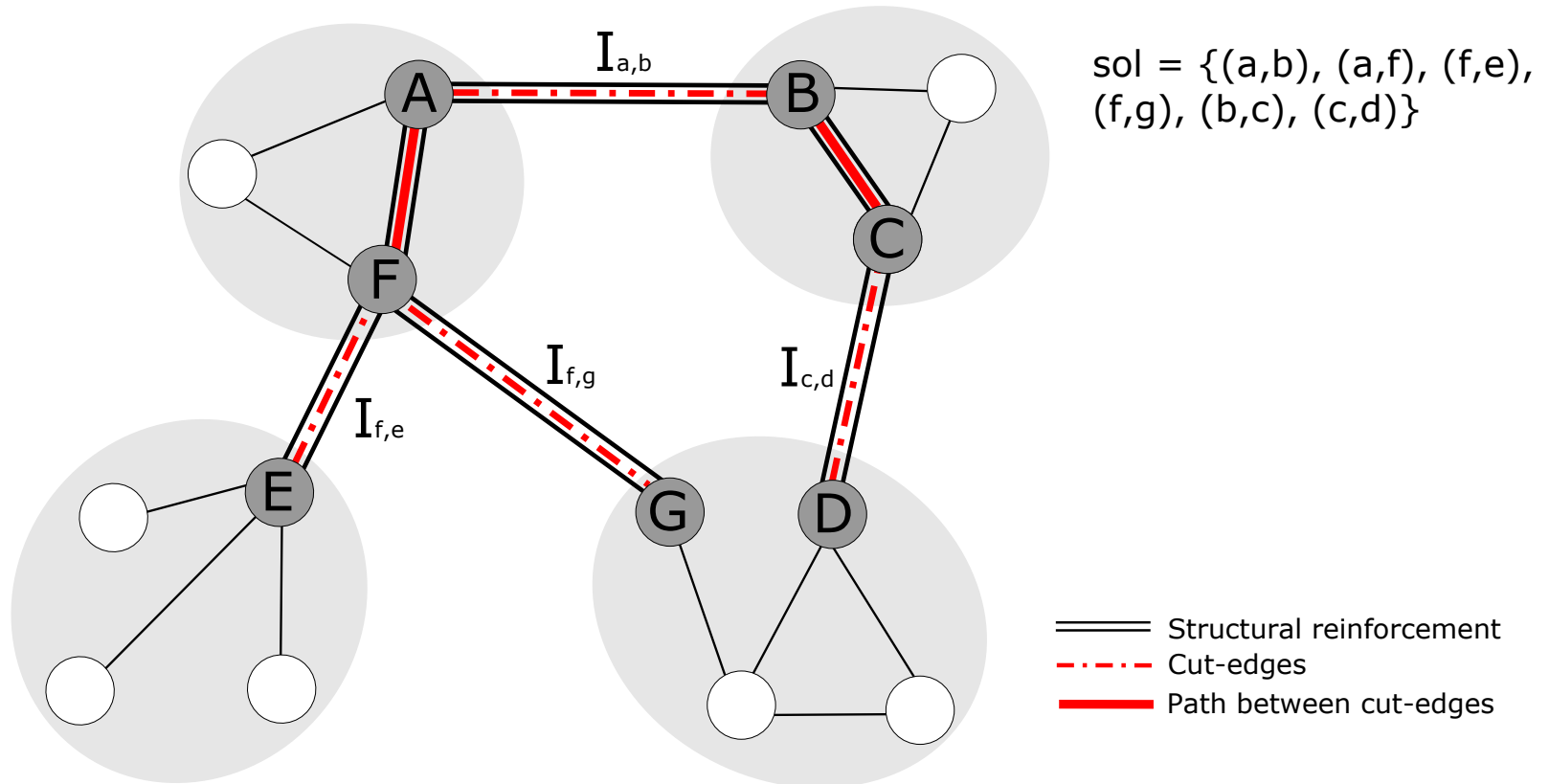
## Example



1. Which elements to expand?
2. How much to invest?

# InP Network Expansion: Overview

## Example



# InP Network Expansion: Exact Model

- Problem constraints
  - Router capacity (memory and CPU)
  - Link capacity (bandwidth)
  - Expansion costs (routers and links)
  - Creation of a new core, acting as a structural reinforcement
  - Ensures the investment will not exceed the available funds of the InP (growth)
  - Ensures that only a subset of physical devices will be affected by the expansion procedure (coverage)
- **Objective:** maximize reconnection between the most important cut-edges

# InP Network Expansion: Heuristic

- Similar to the minimum Steiner tree problem, which is known to be NP-hard
- Two-step heuristic:
  1. Identify which devices need to be expanded
  2. Define a strategy for resource distribution among the selected devices
    - Uniformly
    - Probabilistic distribution

# InP Network Expansion: Heuristic

For each **time unit**:

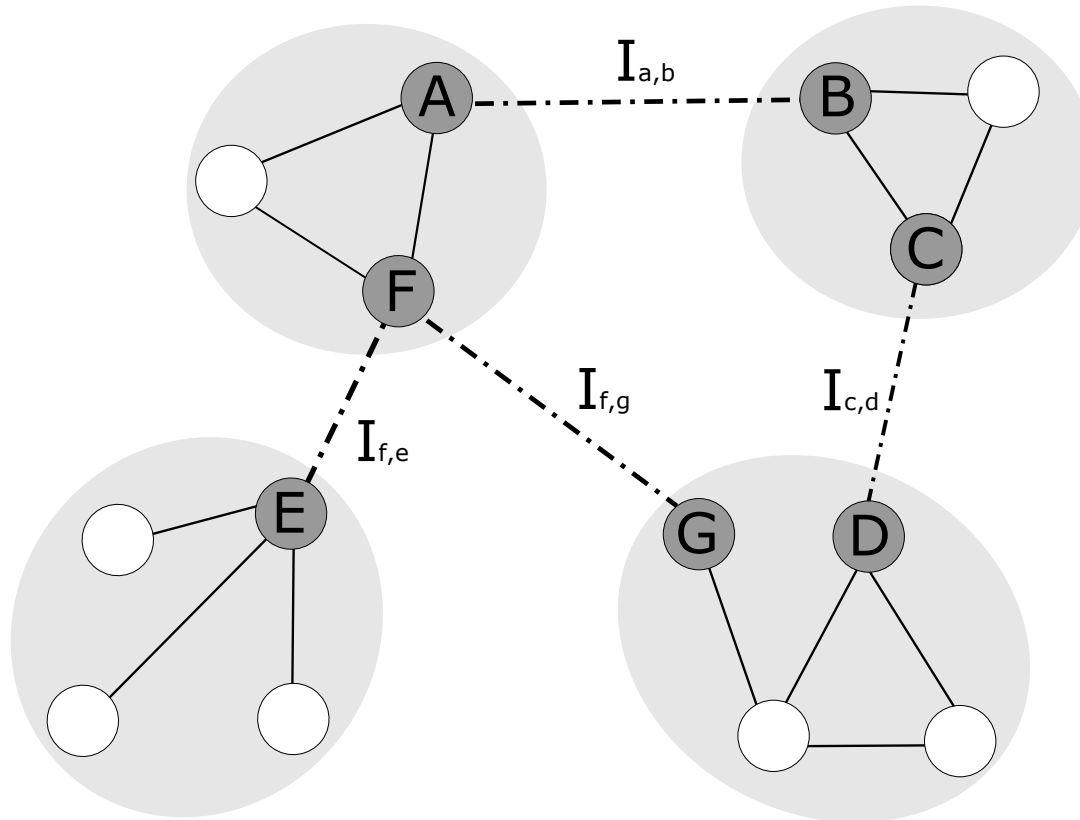
1. Identify and store the set of partitions, as well as the cut-links

If **expansion periodicity**:

1. Compute the importance of each element stored so far
2. Sort accordingly to its importance
3. Select a percentage % of cut-links with highest importance
4. Create a subgraph from such select links
5. MST(subgraph)
6. If  $|\text{subgraph}| > \text{coverge}$ :
  1. Remove the least relevant cut-link from subgraph
7. Else:
  1. Stop

Suggest link/router expansion

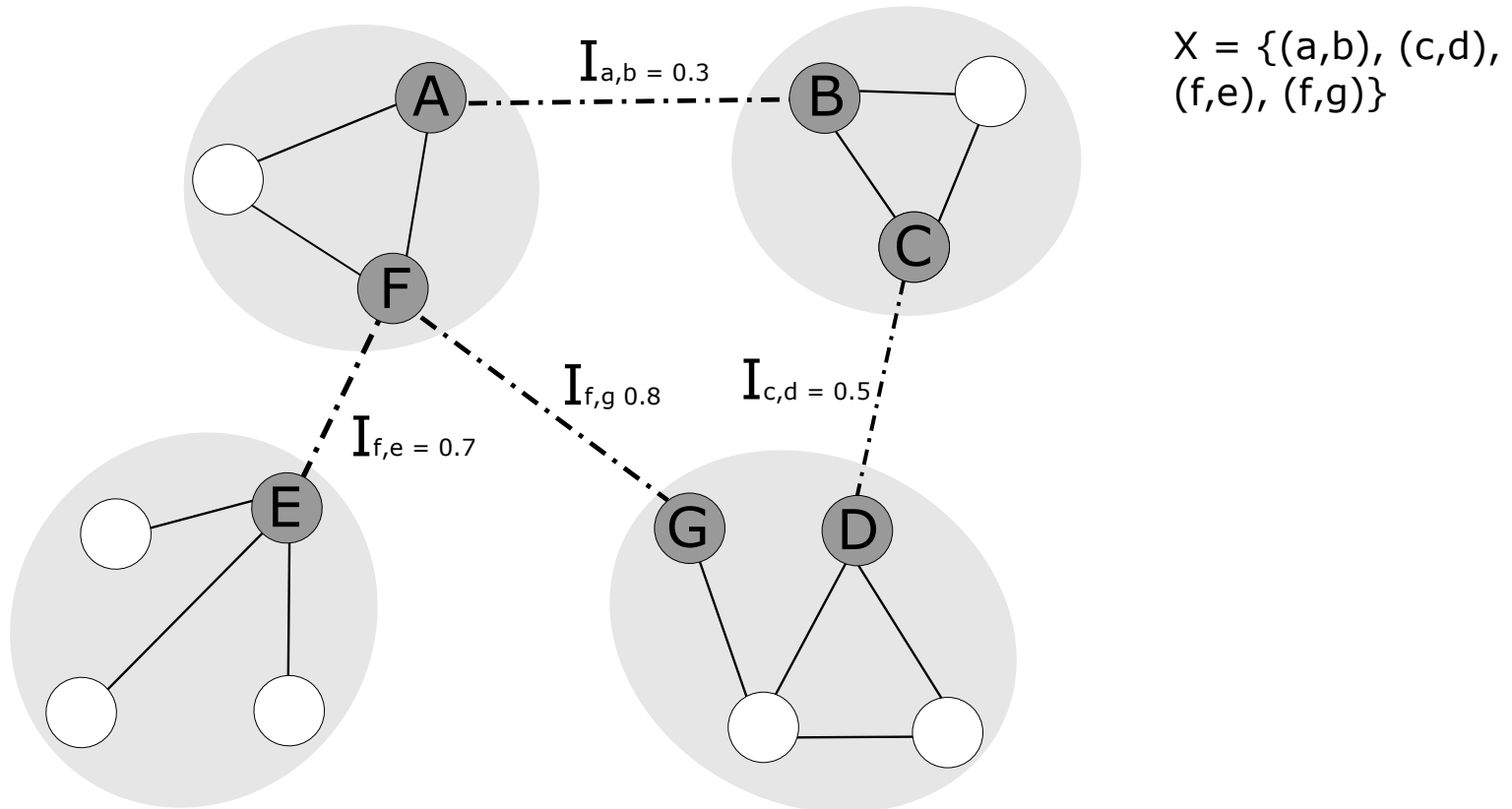
# InP Network Expansion: Heuristic



$X = \{(a,b), (c,d), (f,e), (f,g)\}$

1. Identify and store the set of partitions, as well as the cut-links

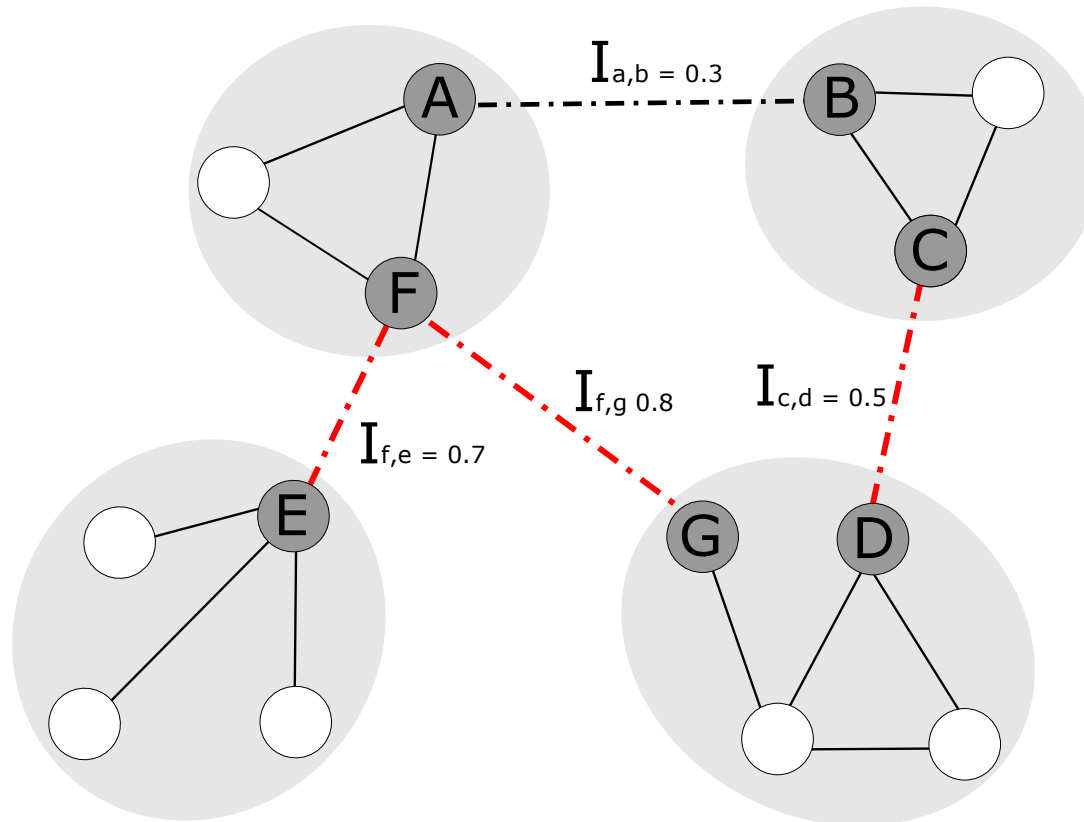
# InP Network Expansion: Heuristic



2. Compute the importance of each element stored so far



# InP Network Expansion: Heuristic

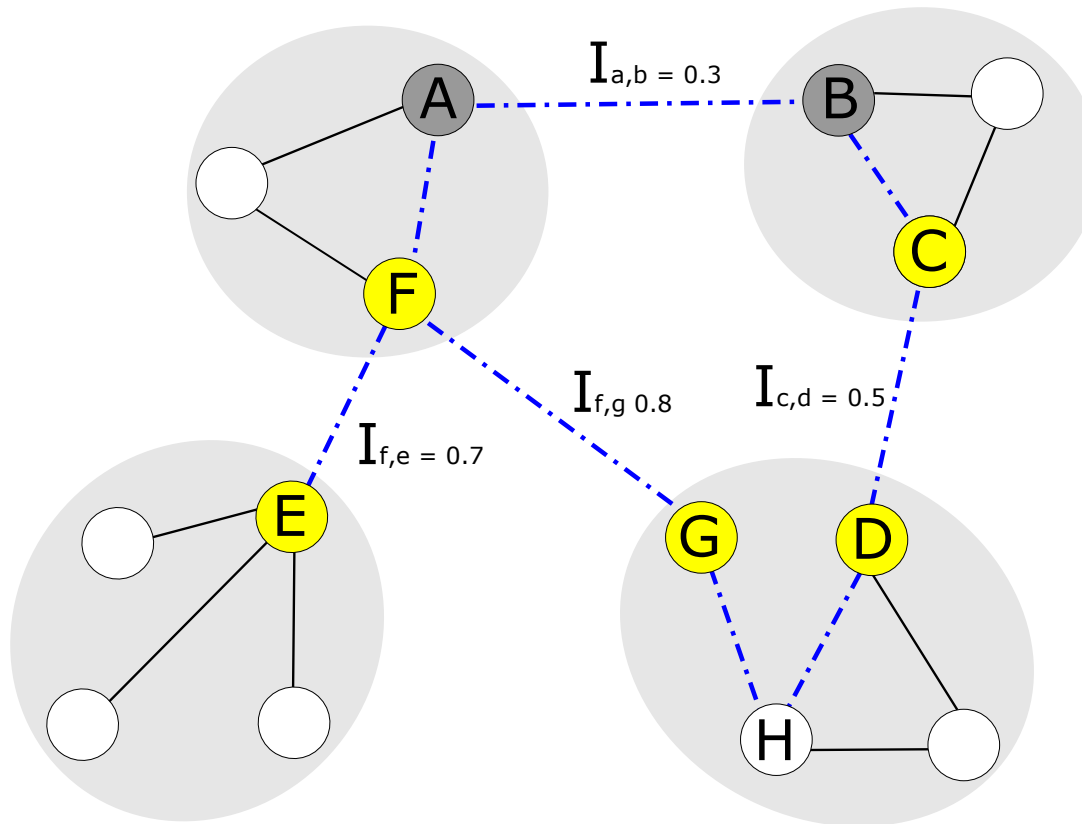


$X = \{(a,b), (c,d), (f,e), (f,g)\}$

20% of coverage

3. Sort accordingly to its importance
4. Select a percentage % of cut-links with highest importance

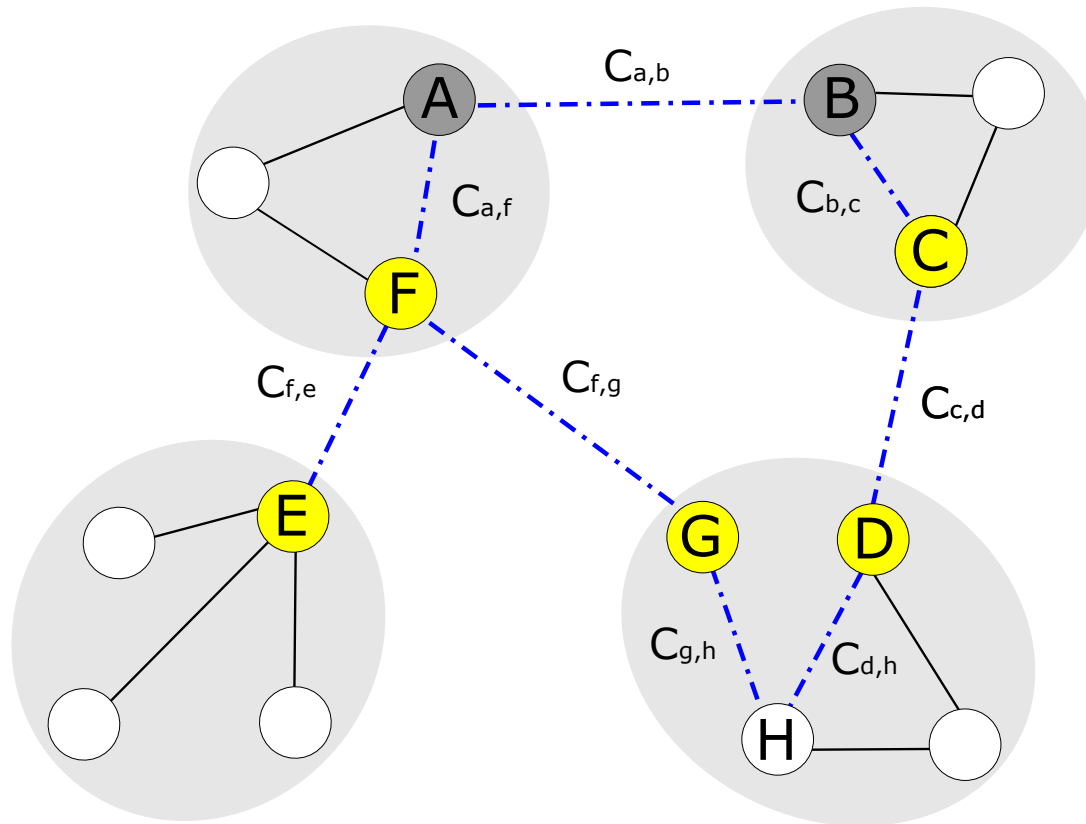
# InP Network Expansion: Heuristic



$X = \{(a,b), (c,d), (f,e), (f,g)\}$   
 $N = \{A,B,C,D,E,F\}$   
 $E = \{(a,b), (c,d), (f,e), (f,g), (a,f), (b,c), (g,h), (h,d)\}$

5. Create a subgraph from such selected elements

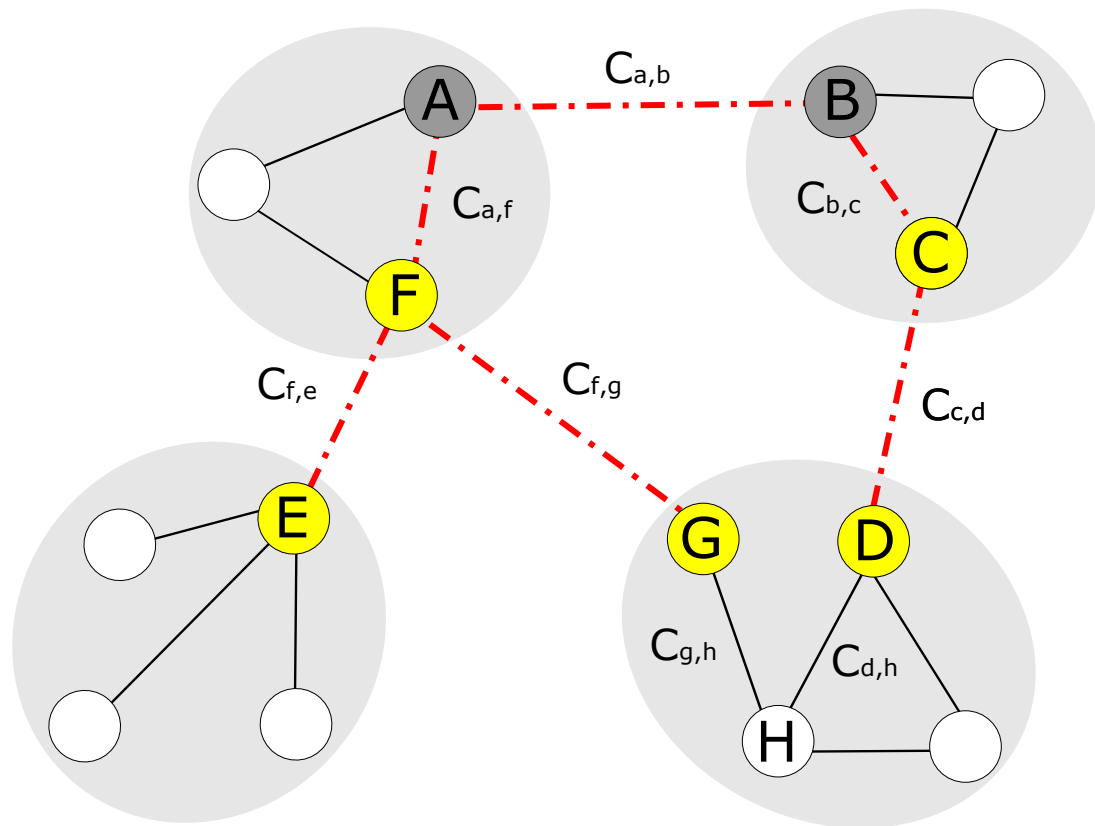
# InP Network Expansion: Heuristic



$X = \{(a,b), (c,d), (f,e), (f,g)\}$   
 $N = \{A,B,C,D,E,F\}$   
 $E = \{(a,b), (c,d), (f,e), (f,g), (a,f), (b,c), (g,h), (h,d)\}$

5. Create a subgraph from such selected elements

# InP Network Expansion: Heuristic



$\text{sol} = \{(a,b), (c,d), (f,e), (f,g), (a,f), (b,c)\}$

6.  $\text{sol} = \text{mst}(\text{subgraph})$
  7. If  $|\text{sol}| > \text{coverage}$ :  
Remove the least relevant cut-link from subgraph
- Else:**  
Stop

20% of coverage?

# Evaluation

## Parameter Selection

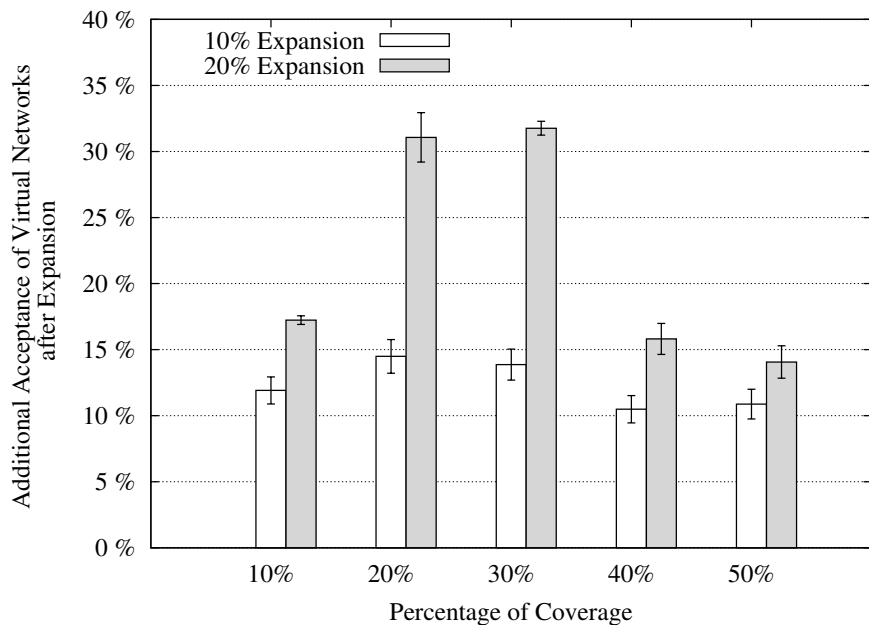
- General Parameters
  - 360 time units
  - 3 VN request at each time unit
  - VNE model proposed by Luizelli et al. [2013]
- Physical Network
  - Topology: *Hub & Spoke*
  - 50 routers: 100% CPU and 256 MB
  - Links: 10 Gbps

# Evaluation

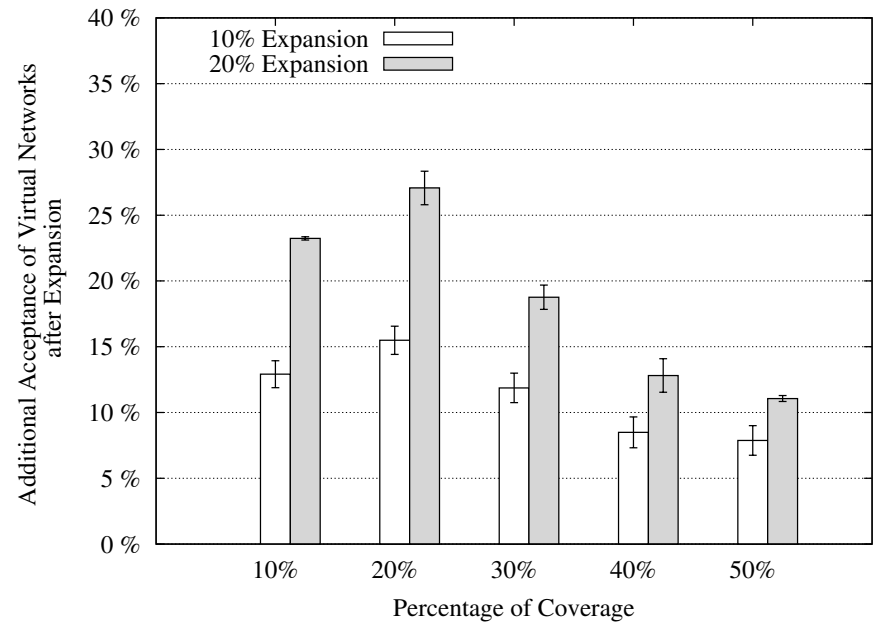
## Parameter Selection

- Virtual Network
  - Topologies: ring and random
  - 5 routers: 20% CPU and 48 MB
  - Links: 2.5 Gbps
- Expansion Strategy
  - Periodicity:
    - Expansion at 180<sup>a</sup> time unit
    - Consecutively expansions
  - Homogeneous costs
  - Coverage: 10% to 50%
  - Investment: 10% and 20%
- Each experiment was run 30 times
- 95% confidence level

# Evaluation Results



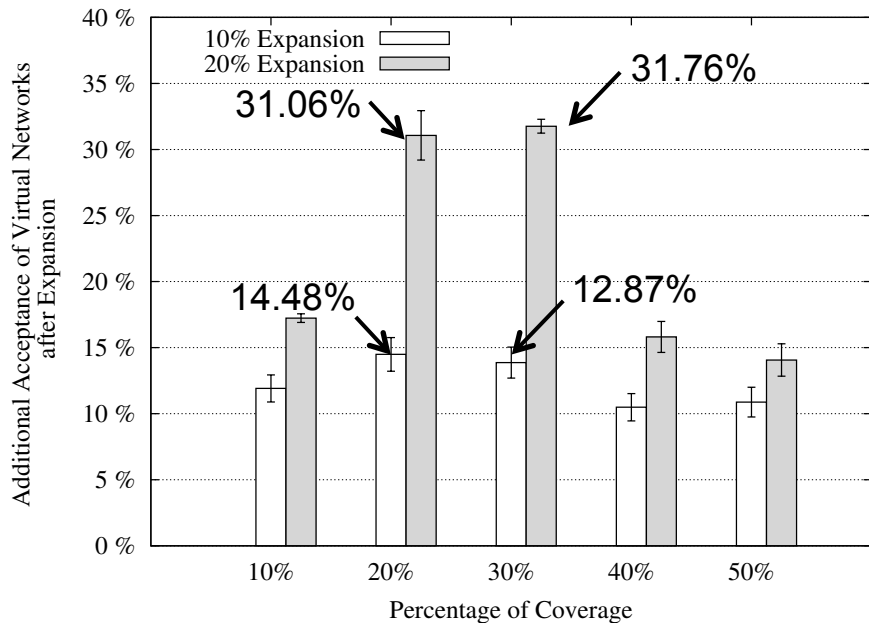
(a) Experiments considering VNs with ring topology.



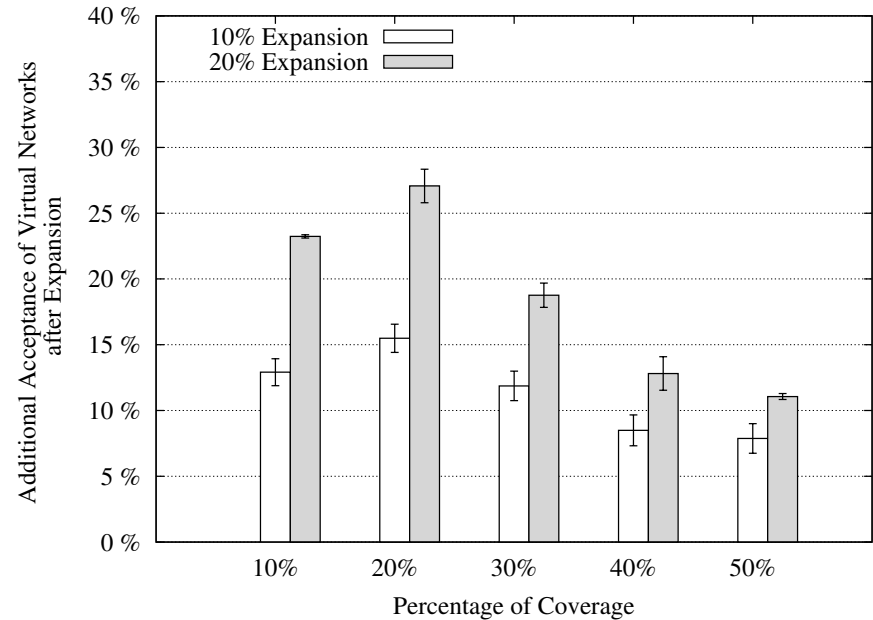
(b) Experiments considering VNs with random topology.

Average increase in virtual network acceptance after the employment of the expansion strategy.

# Evaluation Results



(a) Experiments considering VNs with ring topology.

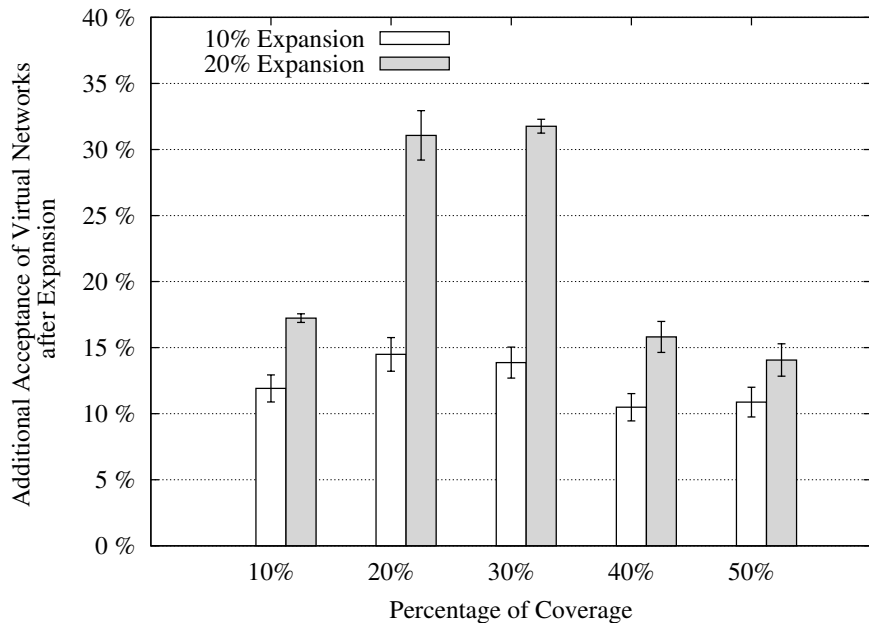


(b) Experiments considering VNs with random topology.

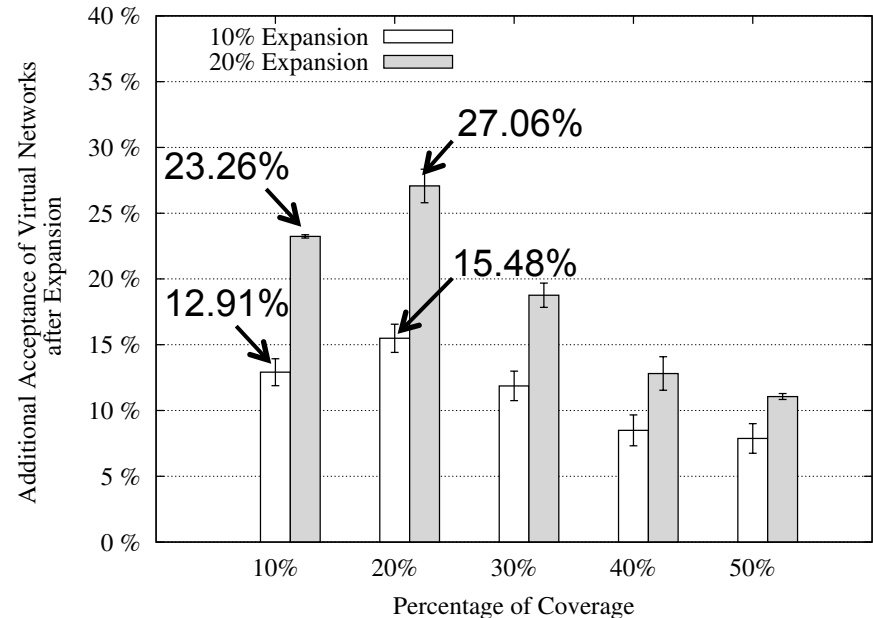
Average increase in virtual network acceptance after the employment of the expansion strategy.



# Evaluation Results



(a) Experiments considering VNs with ring topology.

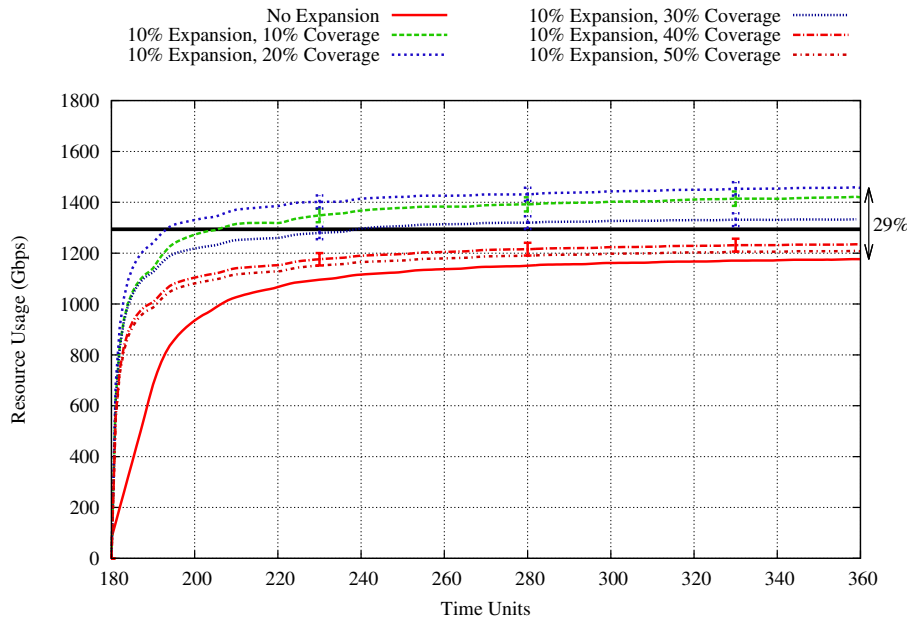


(b) Experiments considering VNs with random topology.

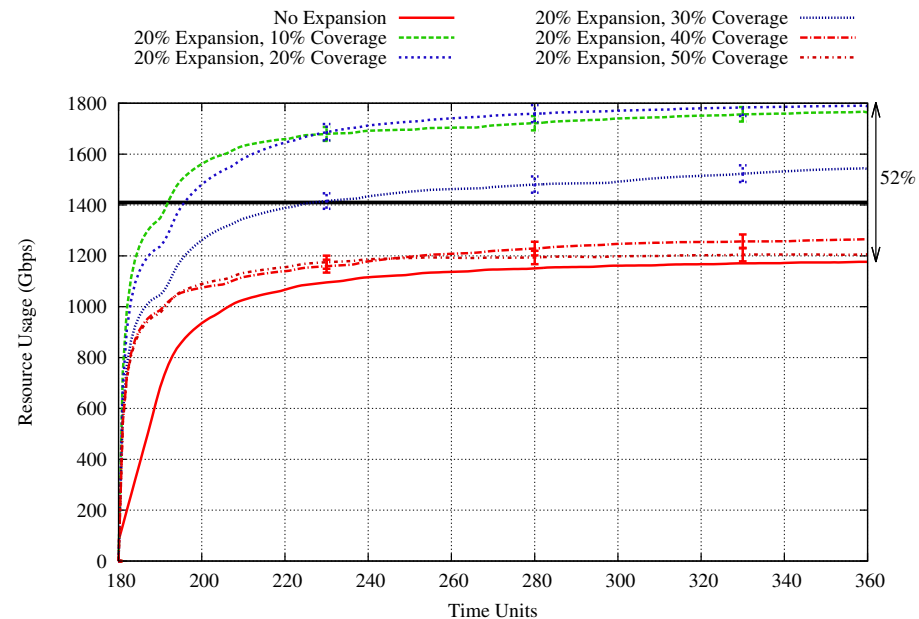
Average increase in virtual network acceptance after the employment of the expansion strategy.

# Evaluation

## Results – Resource Consumption / Random Topology



(a) Experiments considering an expansion of 10%.

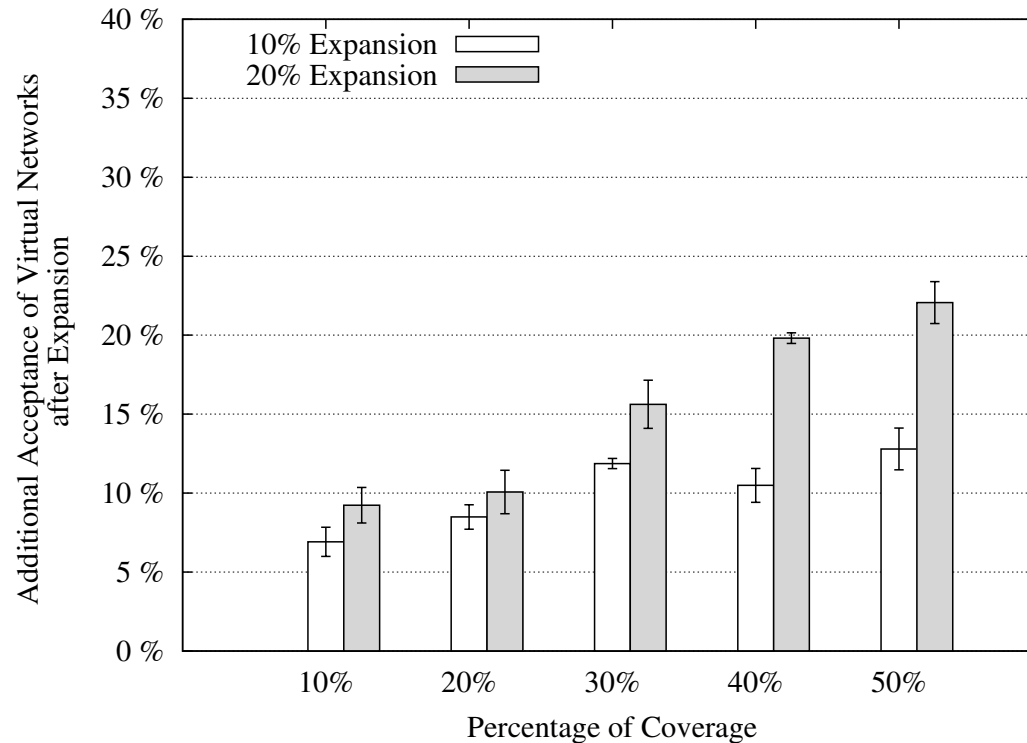


(b) Experiments considering an expansion of 20%.

Overall physical bandwidth usage after the expansion, considering virtual networks with random topology.

# Evaluation

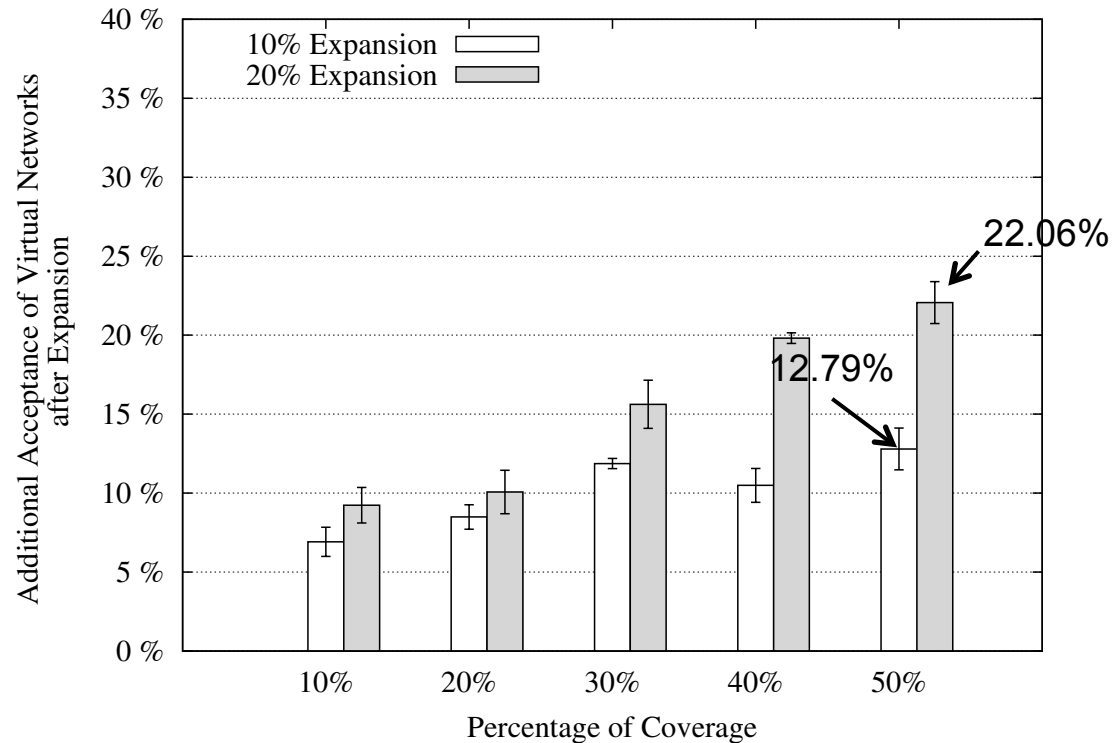
## Results



Average increase in virtual network acceptance after consecutive employments of the expansion strategy.

# Evaluation

## Results



Average increase in virtual network acceptance after consecutive employments of the expansion strategy.

# Conclusion and Future Work

- The expansion strategy performed by our solution leads to:
  - A **sustained increase of up 30%** in virtual network acceptance
  - As well as up to **52% in resource utilization** compared to the original network
- Extending the evaluation
  - Apply it to other backbones topologies
  - Evaluate and propose novel strategies for resource distribution among infrastructure devices
  - Conduct an in-depth analysis of the inter-relationship between its parameters

# Thanks!

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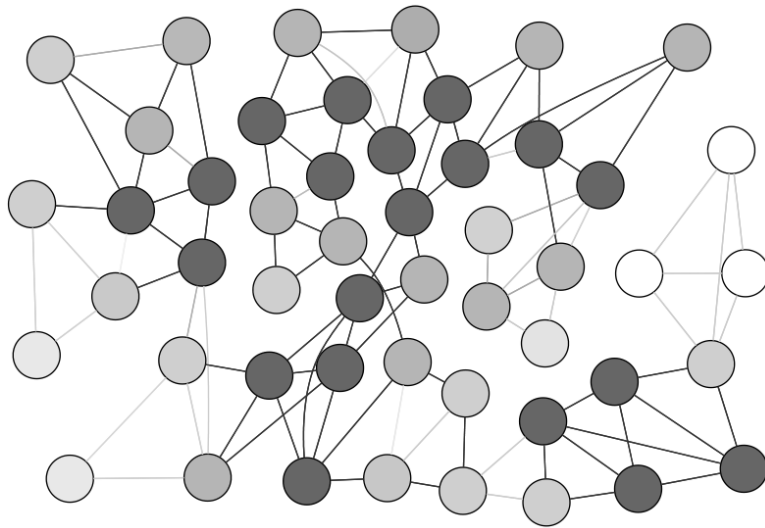
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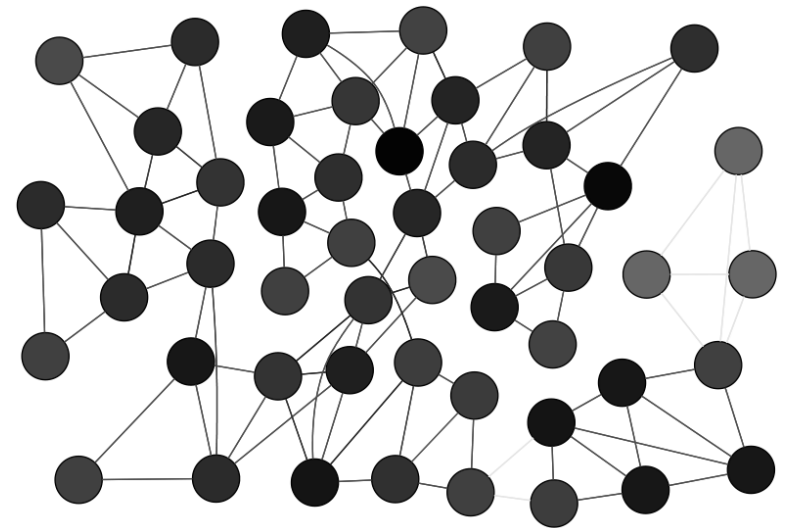


# Evaluation

## Results



(a) Resource usage before expansion.

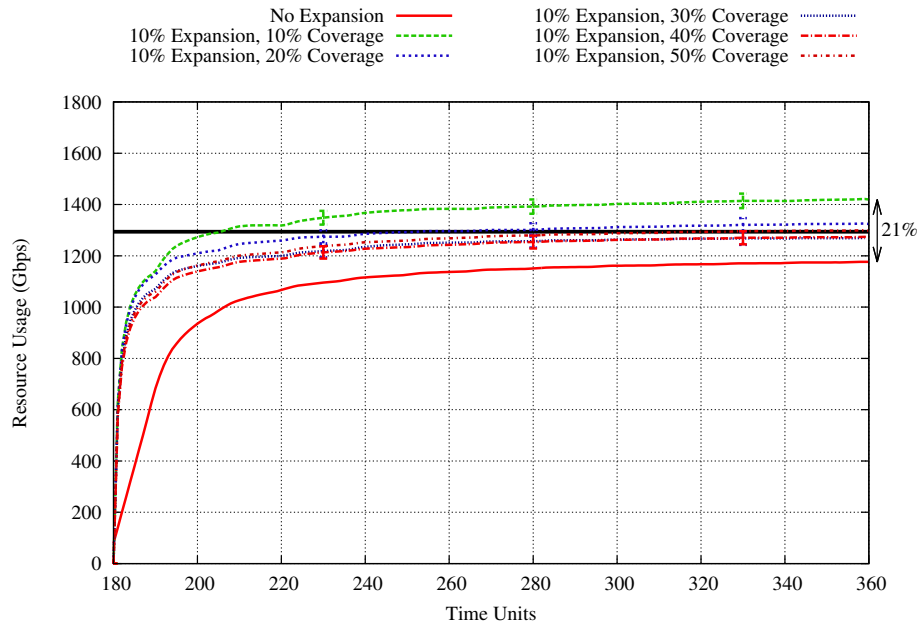


(b) Resource usage after expansion.

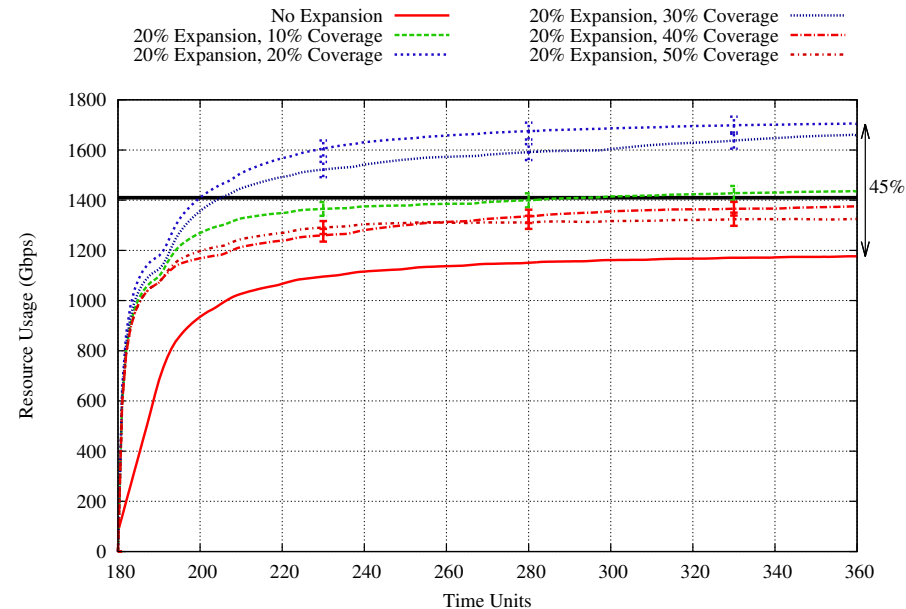
Graphical representation of average infrastructure resource usage before (a) and after (b) an expansion of 20% of resources with coverage of 20%. Darker shades represent higher resource usage.

# Evaluation

## Results – Resource Consumption / Ring Topology



(a) Experiments considering an expansion of 10%.



(b) Experiments considering an expansion of 20%.

Overall physical bandwidth usage after the expansion, considering virtual networks with ring topology.

# Optimal Model for Virtual Network

Objective function:

$$\min \sum_{(i,j) \in L^P} \sum_{r \in N^V, (k,l) \in L^V} A_{i,j,r,k,l}^L B_{r,k,l}^V$$

Subject to:

$$\sum_{r \in N^V, j \in R^V} C_{r,j}^V A_{i,r,j}^R \leq C_i^P \quad \forall i \in R^P \quad (R1)$$

$$\sum_{r \in N^V, j \in R^V} M_{r,j}^V A_{i,r,j}^R \leq M_i^P \quad \forall i \in R^P \quad (R2)$$

# Optimal Model for Virtual Network

$$\sum_{r \in N^V, (k,l) \in L^V} B_{r,k,l}^V A_{i,j,r,k,l}^L \leq B_{i,j}^P \quad \forall (i,j) \in L^P \quad (R3)$$

$$\sum_{i \in R^P} A_{i,r,j}^R = 1 \quad \forall r \in N^V, j \in R^V \quad (R4)$$

$$\sum_{j \in R^V} A_{i,r,j}^R \leq 1 \quad \forall i \in R^P, r \in N^V \quad (R5)$$

# Optimal Model for Virtual Network

$$\sum_{j \in R^P} A_{i,j,r,k,l}^L - \sum_{j \in R^P} A_{j,i,r,k,l}^L = A_{i,r,k}^R - A_{i,r,l}^R \quad \forall r \in N^V, (k,l) \in L^V, i \in R^P \quad (R6)$$

$$jA_{i,r,k}^R = lA_{i,r,k}^R \quad \forall (i,j) \in S^P, r \in N^V, (k,l) \in S^V \quad (R7)$$

$$A_{i,r,j}^R = E_{i,r,j}^R \quad \forall (i,r,j) \in E^R \quad (R8)$$

$$A_{i,j,r,k,l}^L = E_{i,j,r,k,l}^L \quad \forall (i,j,r,k,l) \in E^L \quad (R9)$$

# InP Expansion Model

$$\begin{aligned} \text{CustoExp} = & \sum_{e \in L^P} x_b \cdot \text{costBw}^P e \\ & + \sum_{i \in R^P} (x_{c_i} \cdot \text{costCPU}^P i + x_{m_i} \cdot \text{costMem}^P i) \end{aligned} \quad (5.1)$$

$$x_e \cdot \left( B_{i,j}^P + \frac{\text{CapitalDisp} \cdot \text{Cobertura}}{\text{costBw}_{i,j}^P} \right) \leq EB_{i,j}^P \quad \forall e \in L^P \quad (5.2)$$

$$x_{i,j} \cdot \left( C_i^P + \frac{\text{CapitalDisp} \cdot \text{Cobertura}}{\text{costCpu}_i^P} \right) \leq EC_i^P \quad \forall (i,j) \in L^P \quad (5.3)$$

$$x_{i,j} \cdot \left( M_i^P + \frac{\text{CapitalDisp} \cdot \text{Cobertura}}{\text{costMem}_i^P} \right) \leq EM_i^P \quad \forall (i,j) \in L^P \quad (5.4)$$

# InP Expansion Model

$$\text{CustoExp} \leq \text{CapitalDisp} \quad (5.5)$$

$$\sum_{a \in \delta^+(u)} x_a^k - \sum_{a \in \delta^-(u)} x_a^k = \begin{cases} 1 \cdot q_u & \text{se } u = s \\ -1 \cdot q_u & \text{se } u = k \\ 0 & u \in R^P / \{s, k\} \end{cases} \quad \forall u \in R^P, \forall k \in R^C \quad (5.6)$$

$$q_u \geq \frac{\sum_{a \in \delta^+(u)} z_a}{|\delta^+(u)|} \quad \forall u \in R^P \quad (5.7)$$

$$\frac{\sum_{e \in L^P} x_e}{|L^P|} \leq \text{Cobertura} \quad (5.8)$$

$$\text{Maximize} \sum_{e \in X} I_e \cdot z_e \quad (5.9)$$

# HIPER: Detailed Algorithm

**Input:** Capital disponível, Percentual de cobertura, Periodicidade da expansão, Infraestrutura física do InP  $N$ , Mapeamento das redes virtuais  $A_{i,r,j}^R$  and  $A_{i,j,r,k,l}^L$

**Output:** Conjunto de dispositivos físicos a serem expandidos

```
1  $X \leftarrow \emptyset$ 
2  $F \leftarrow \emptyset$ 
3  $C \leftarrow \emptyset$ 
4 foreach UnidadeTempo do
5    $particoes \leftarrow obterConjuntoParticoes(N, E^R, E^L)$ 
6    $X \leftarrow atualizarEnlacesCorte(particoes)$ 
7    $F \leftarrow atualizarFrequencia(X)$ 
8    $C \leftarrow atualizarCobertura(X, particoes)$ 
9   if PeriodicidadeDaExpansao then
10    foreach  $(i, j) \in X$  do
11       $I_{i,j} \leftarrow \frac{F_{i,j}}{\sum_{v(i,j)} F_{v,j}} \cdot C_{i,j}$ 
12    end
13    while true do
14       $ordenaDesc(X, I)$ 
15       $list \leftarrow seleciona \% \text{ dos enlaces de } X \text{ (\% igual ao percentual de cobertura)}$ 
16       $R^c \leftarrow roteadores \text{ de } list$ 
17       $L^c \leftarrow enlaces \text{ dos caminhos de custo mínimo entre cada par de roteador}$ 
18       $(a, b) \in R^c$ 
19       $N^c = (R^c, L^c)$ 
20       $sol^c \leftarrow mst(N^c)$ 
21      if  $numeroRoteadores(sol^c) > Cobertura$  ou  $numeroEnlaces(sol^c) > Cobertura$  then
22         $X.removeItem()$ 
23      else
24        parar
25      end
26    end
27     $sugiraExpansaoEnlaces(CapitalDisponivel)$ 
28     $sugiraExpansaoRoteadores(CapitalDisponivel)$ 
29     $X \leftarrow \emptyset$ 
30 end
```

**Algoritmo 1:** Visão geral da solução proposta para o problema de expansão de redes de InPs.