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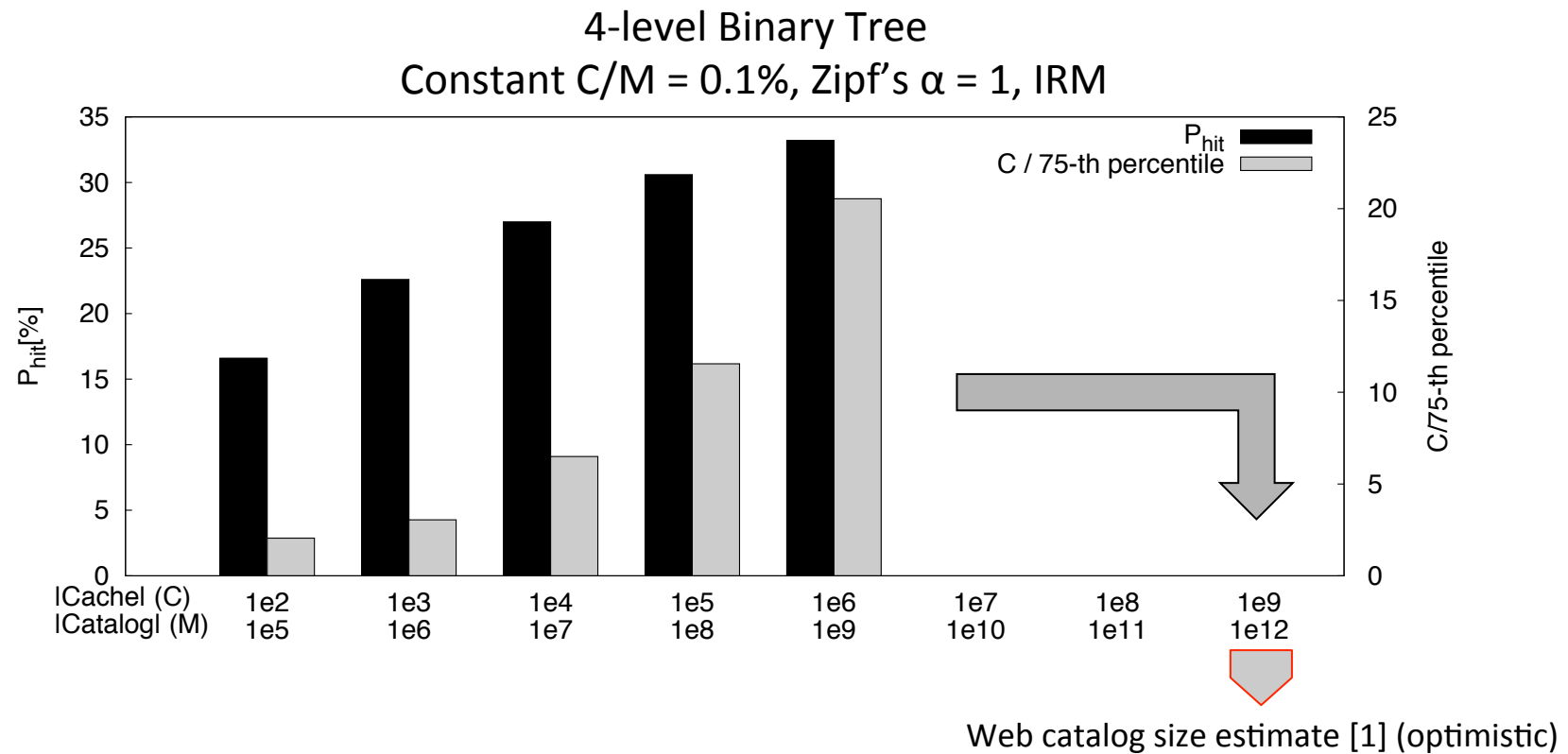
# Model-Graft: Accurate, Scalable and Flexible Analysis of Cache Networks

23rd ICNRG Meeting (Interim) – 14/15-01-2016  
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# MOTIVATION

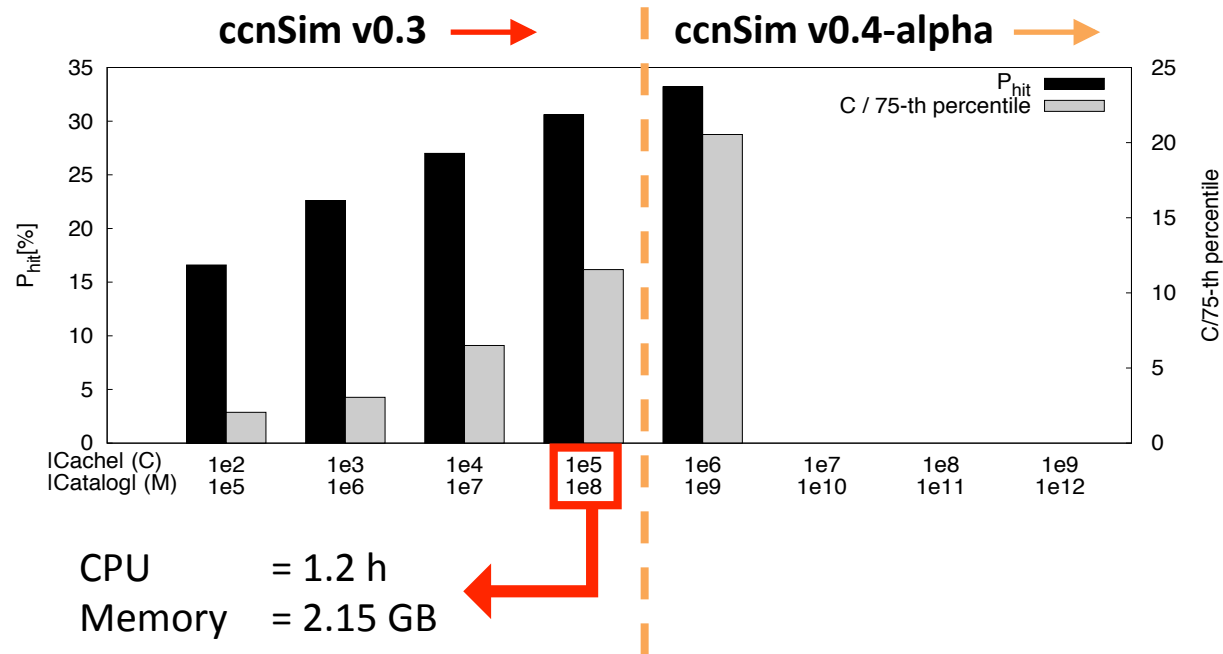
**Simulation** is the primary tool for performance evaluation of cache networks.

Some phenomena only appear @ scale...



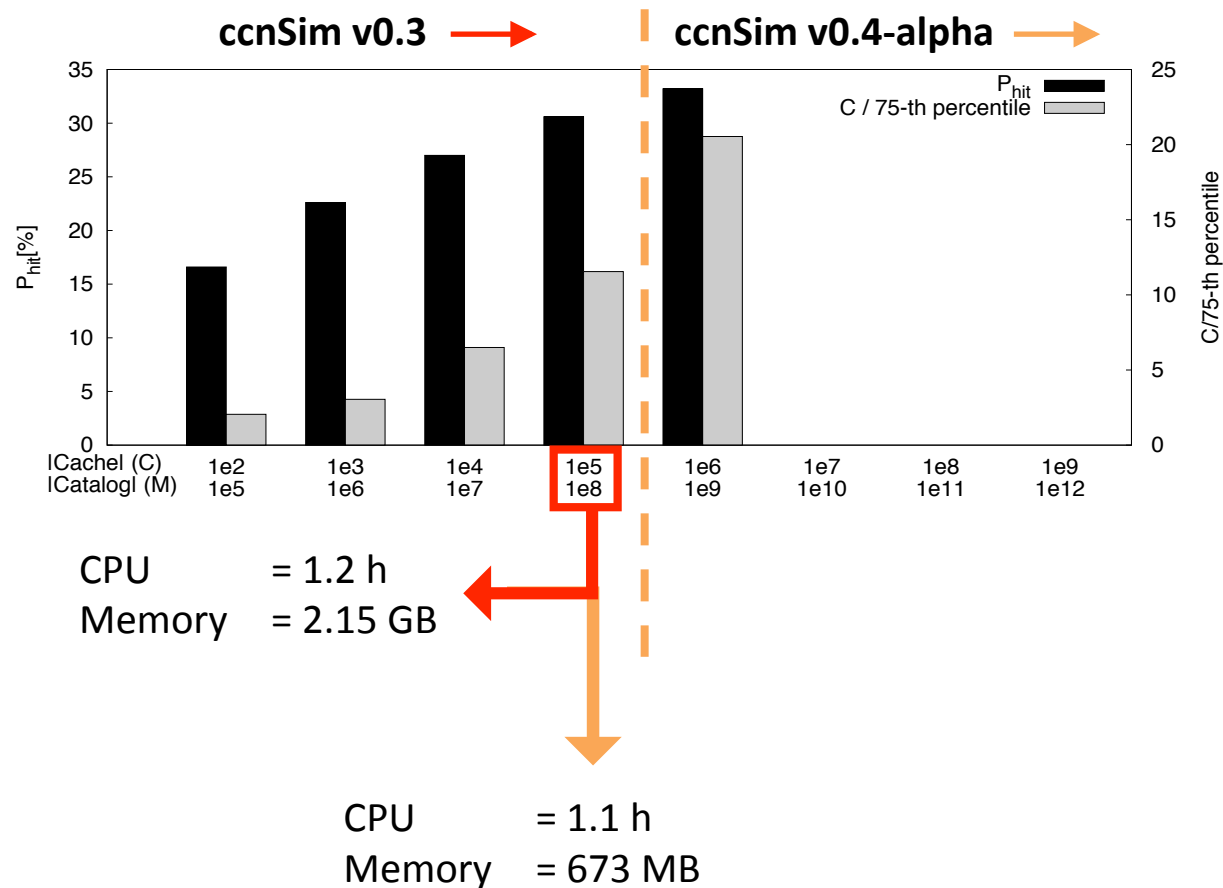
# SIMULATION LIMITATIONS

People have limited CPU & Memory budgets



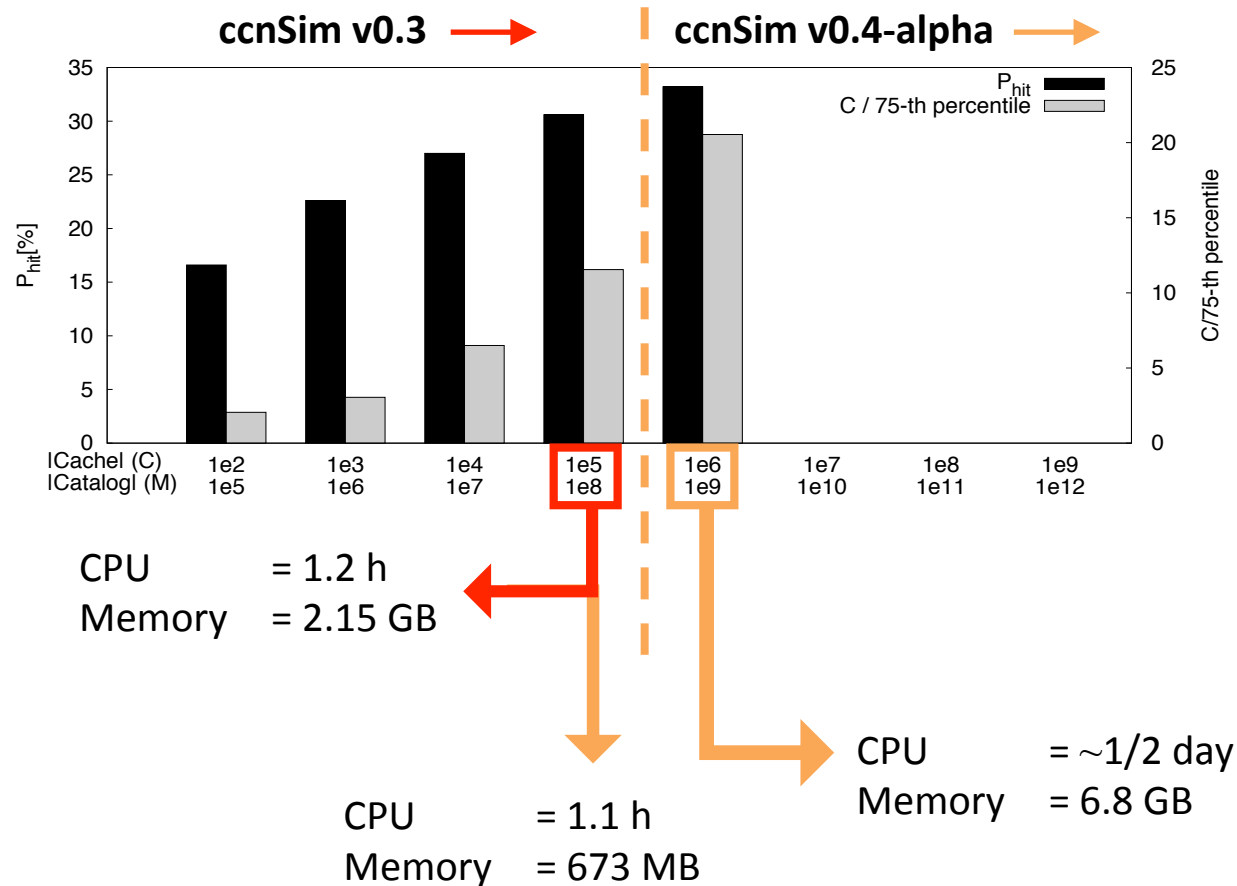
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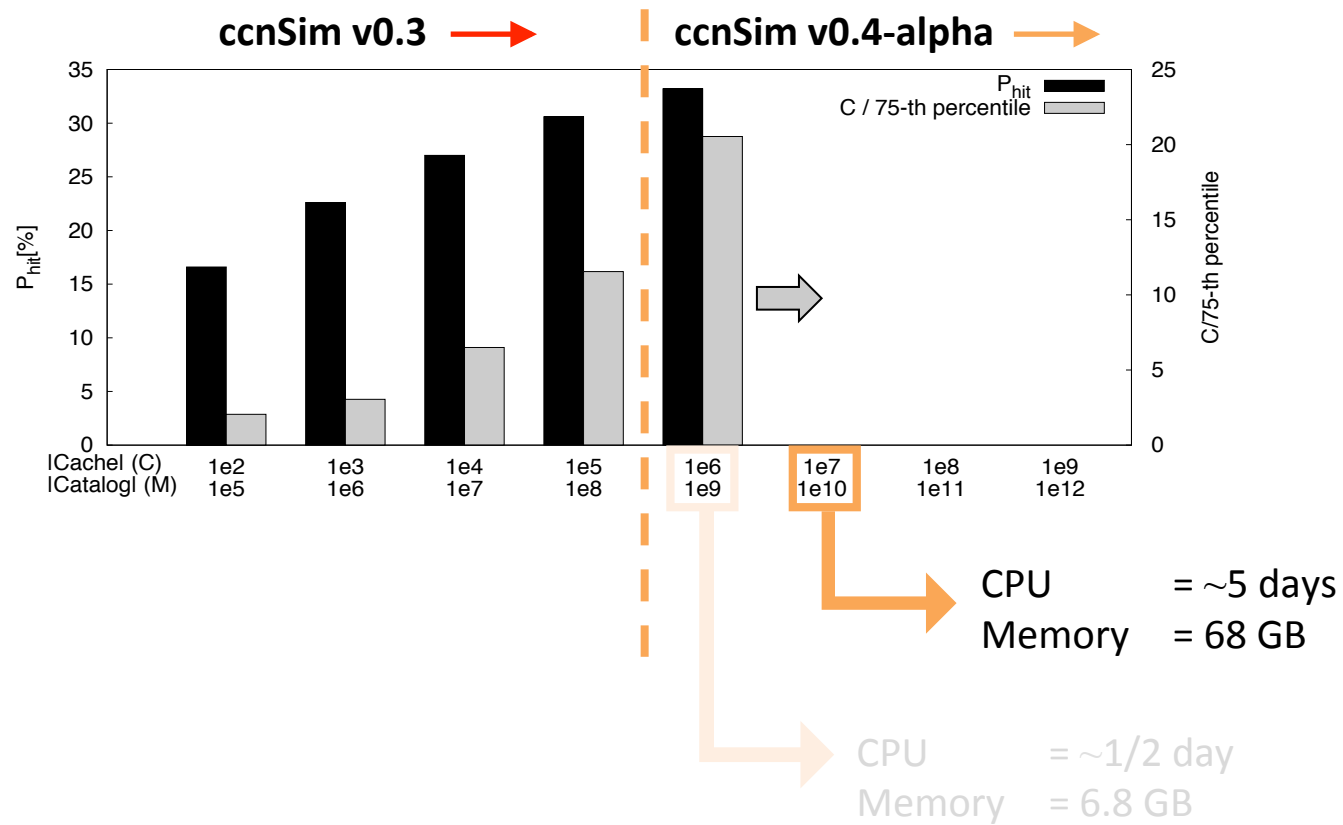
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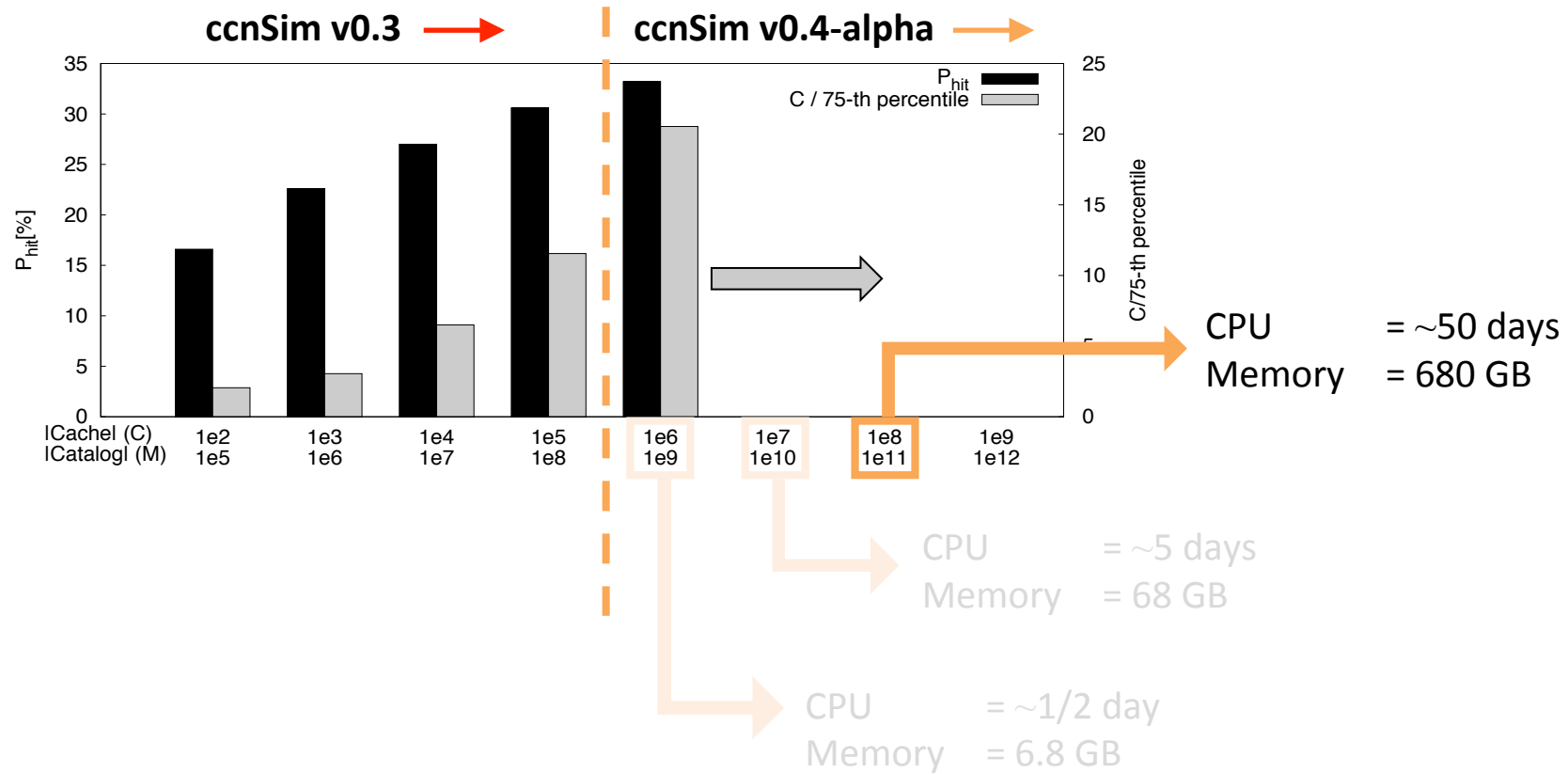
People have limited CPU & Memory budgets



**One order of magnitude more becomes resource expensive**

# SIMULATION LIMITATIONS

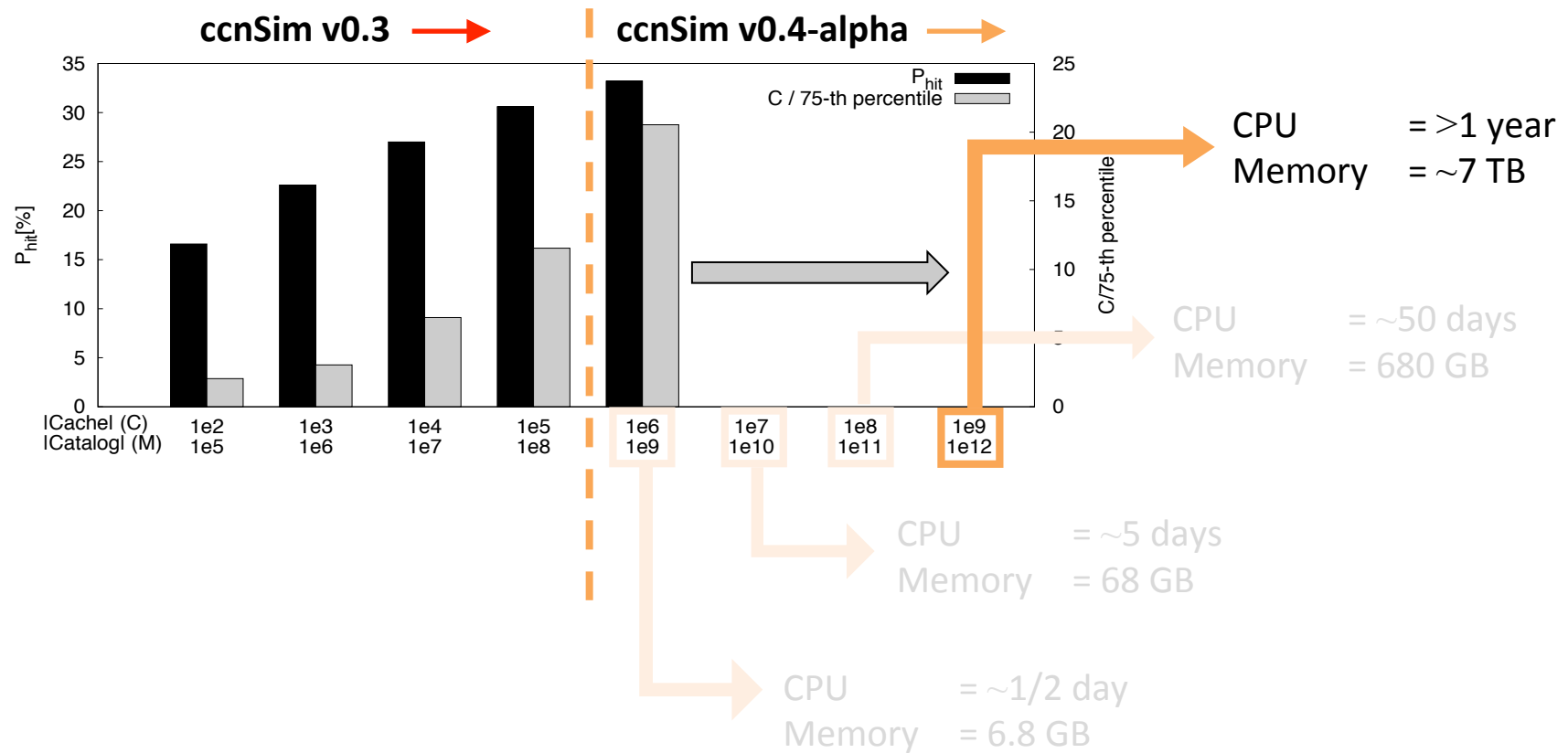
People have limited CPU & Memory budgets



**Two** orders of magnitude more become **really cumbersome**

# SIMULATION LIMITATIONS

People have limited CPU & Memory budgets

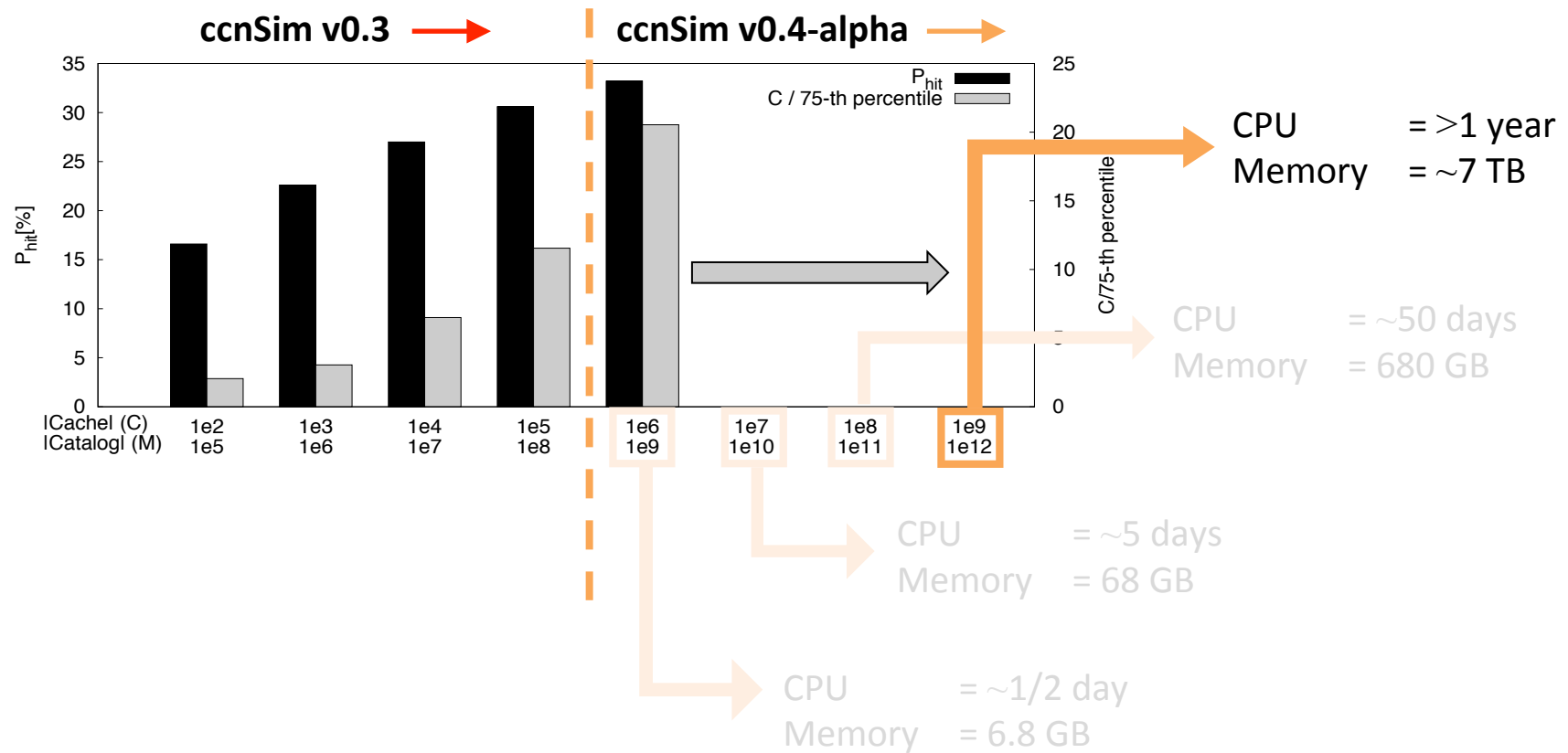


Three orders of magnitude more become **unfeasible**



# SIMULATION LIMITATIONS

People have limited CPU & Memory budgets



- **Event-driven Simulation** → Require careful instrumentation  
→ Massive computing power at large scale  
→ Inefficient (wasting time and memory with expected events)

# IDEA

## GAIN

Time to Live (TTL) caches	+	CPU & Memory
Downscaling M, C, and R with factor $\Delta$	+	CPU & Memory
Rejection Inversion Sampling	+	Memory
Error correction with feedback loop	=	Stability & Accuracy

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Downscaled MonteCarlo  
TTL-based (MC-TTL) Simulation

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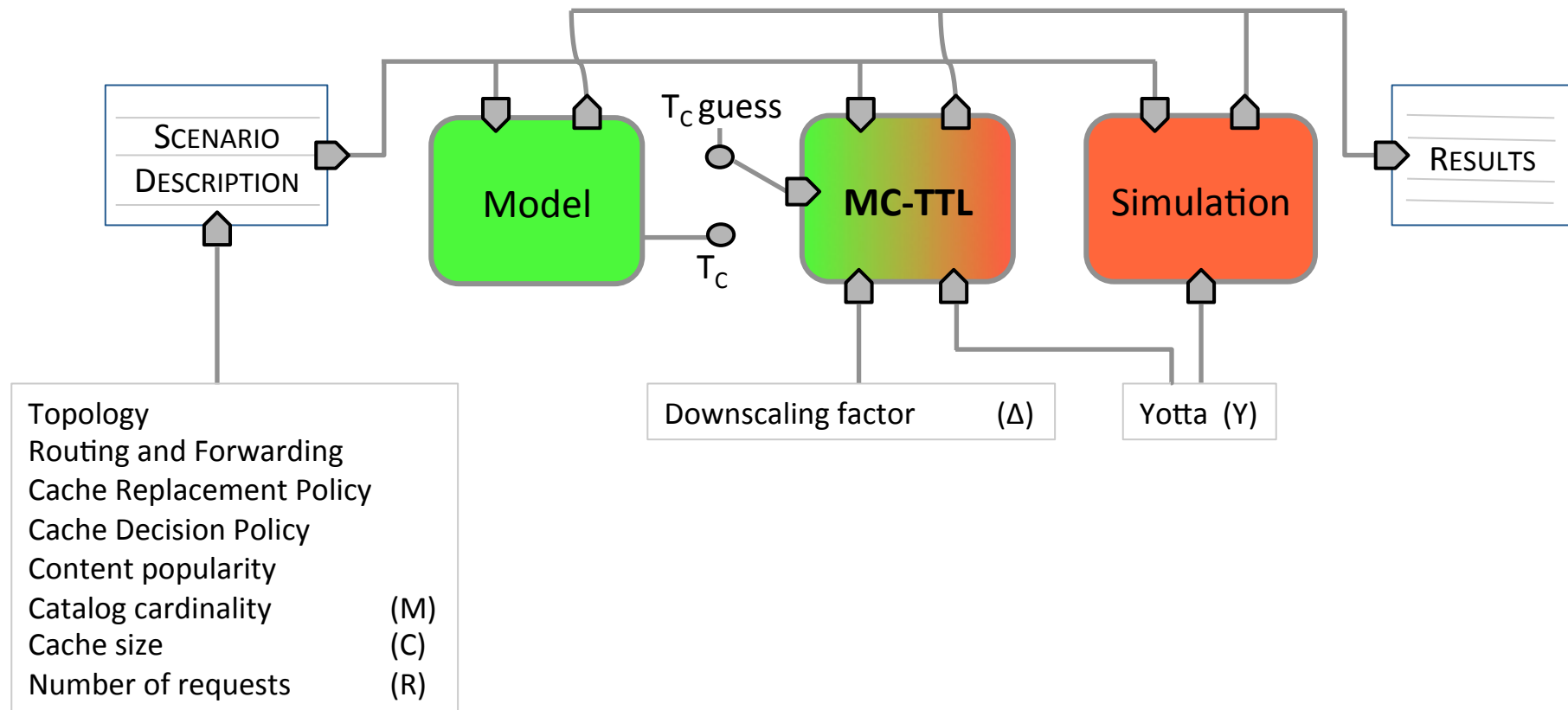
		<b>GAIN</b>
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## Downscaled MonteCarlo TTL-based (MC-TTL) Simulation

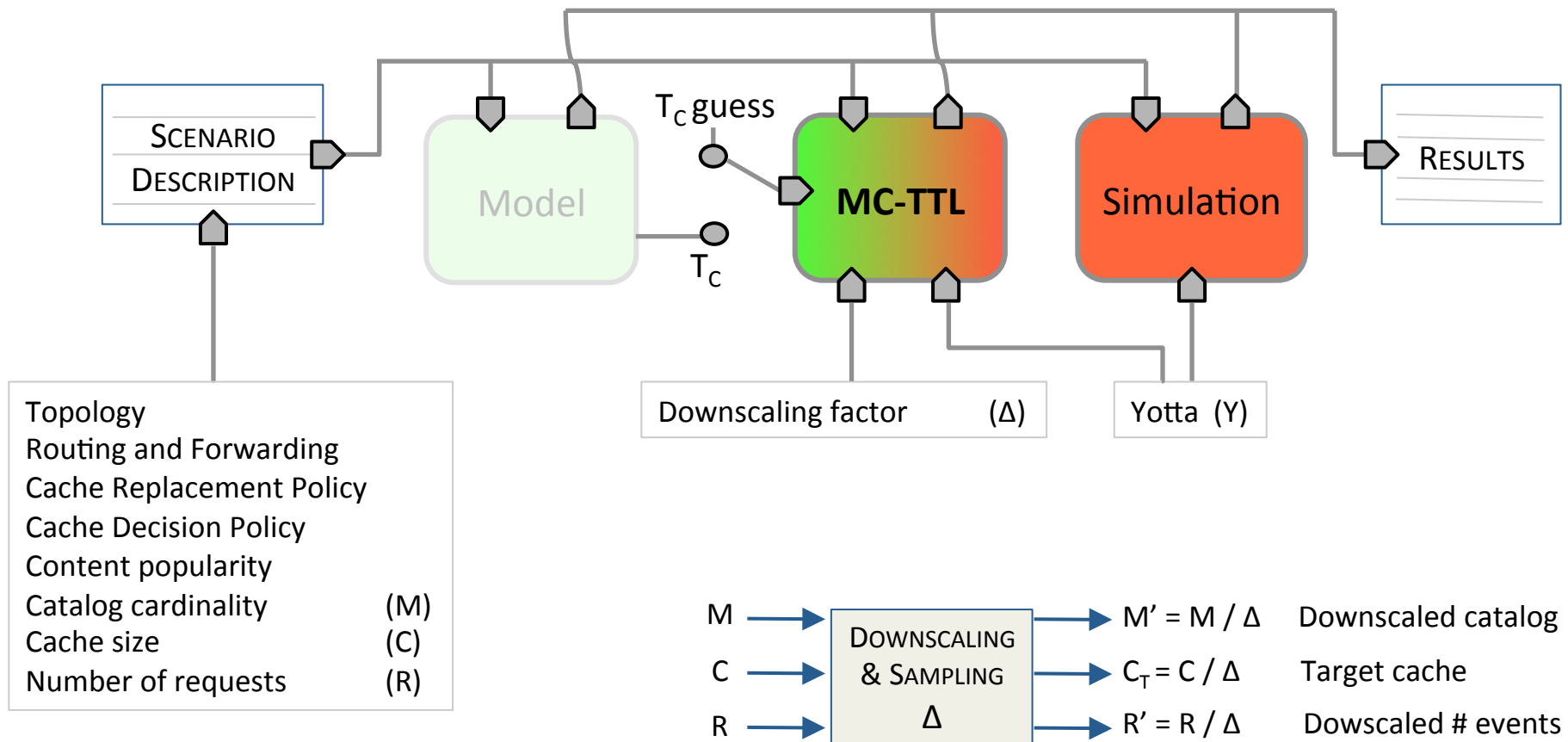
Ex. with  $\Delta=1e5$

**~100x** CPU & Memory gain  
**~2%** Accuracy

# UNDER THE HOOD



# UNDER THE HOOD



Backup slides for technical details



# RESULTS I – VERY LARGE SCENARIO

## 4-level Binary Tree

|Cache| - C = 1e6  
 |Catalog| - M = 1e9      Downscaling Factor - Δ = 1e5  
 # Requests - R = 1e9

Cache Decision Policy		$P_{hit}$	CPU	Gain	Mem [MB]	Gain
<b>LCE</b>	Simulation	33.2	11.4 h	<b>160x</b>	6371	<b>168x</b>
	MC-TTL	31.4	256 s		38	
<b>FIX0.1</b>	Simulation	35.4	7.3 h	<b>90x</b>	6404	<b>168x</b>
	MC-TTL	34.0	291 s		38	
<b>2-LRU</b>	Simulation	37.0	10.8 h	<b>97x</b>	8894	<b>234x</b>
	MC-TTL	36.1	402 s		38	

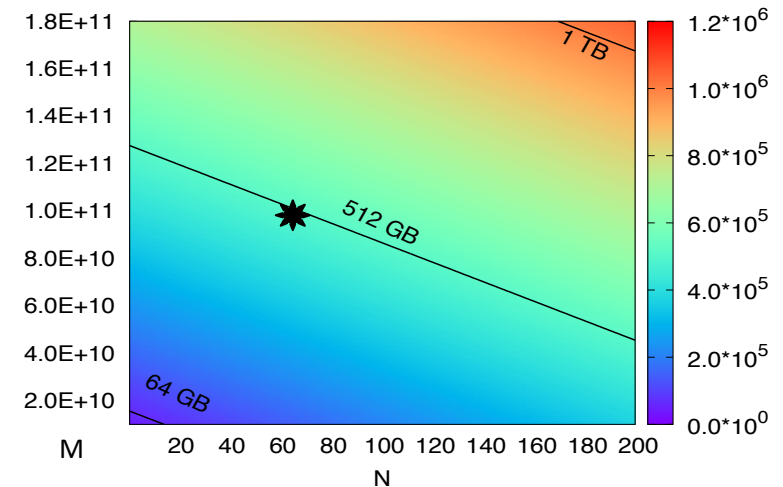
# RESULTS II – WEB SCALE SCENARIO

## Memory Model Fitting (Simulator)

$$\text{Mem} = (1.65 \cdot 10^{-4}) \cdot N \cdot C + 4 \cdot 10^{-6} \cdot M + 19.83 \text{ [MB]}$$

(ccnSim v0.4-alpha with rejection inversion sampling)

- 1 cache entry  $\approx$  165 Bytes
- 1 catalog entry = 4 Bytes
- Fix cost  $\approx$  19.83 MB



\* CDN-like:  $N \sim 60 - M = 1e11 - C = 1e7$

			Technique				
			MC-TTL			Simulation (Est)	
			Mem[MB]	CPU	Cycles	Mem[MB]	CPU
4-level Binary Tree	Parameters	$M=R=1e10 - C=1e6 - \Delta=1e5$	45	0.4 h	1	70000	4.7 days
CDN-like (N=67)		$M=R=1e11 - C=1e7 - \Delta=1e6$	31	12.5 h	3	520000	~50 days

# CONCLUSIONS

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- Extreme scalability, general methodology  
Implementable in every simulator (ndnSIM, Icarus, ...)
- Available in ccnSim v0.4-alpha  
(<http://perso.telecom-paristech.fr/~drossi/ccnSim>)
- Technical Report (slightly old)  
M. Tortelli, D. Rossi and E. Leonardi,  
Model-Graft: Accurate, Scalable and Flexible Analysis of Cache Networks  
*Tech. Rep.* [CCN-TR15], Telecom ParisTech, 2015.

THANK YOU !

QUESTIONS ?

# BACKUP SLIDES

# CHE'S APPROXIMATION

$$T_c(m) = T_c$$

**Cache eviction time** for content  $m$  (i.e., interval of time after which 'm' is evicted)

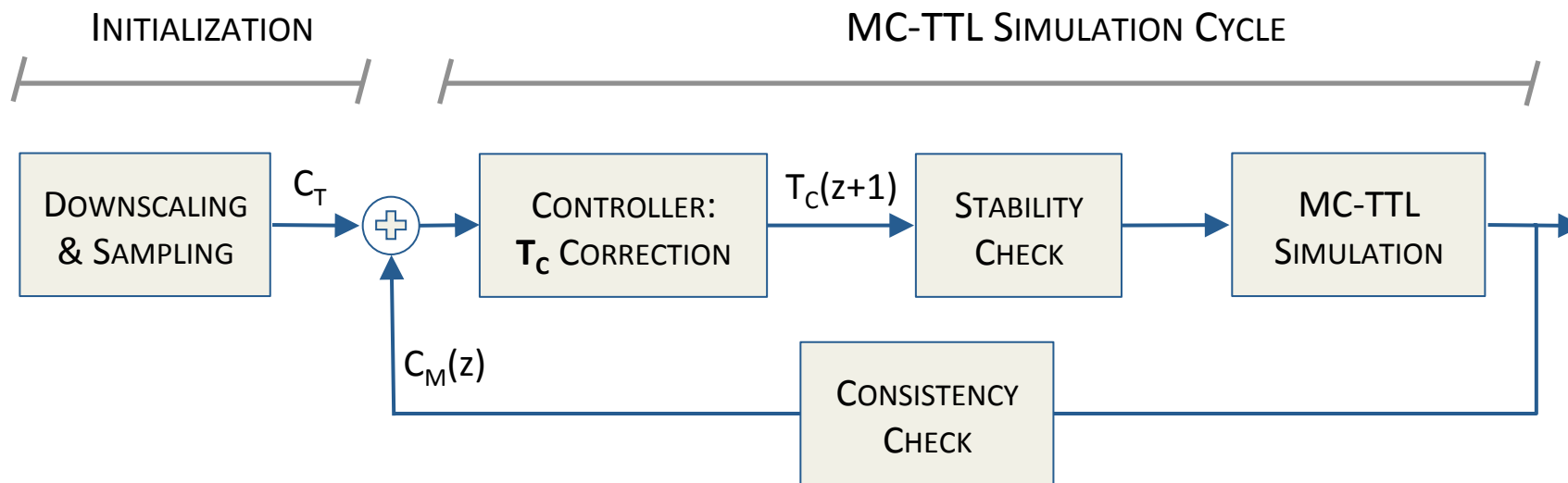
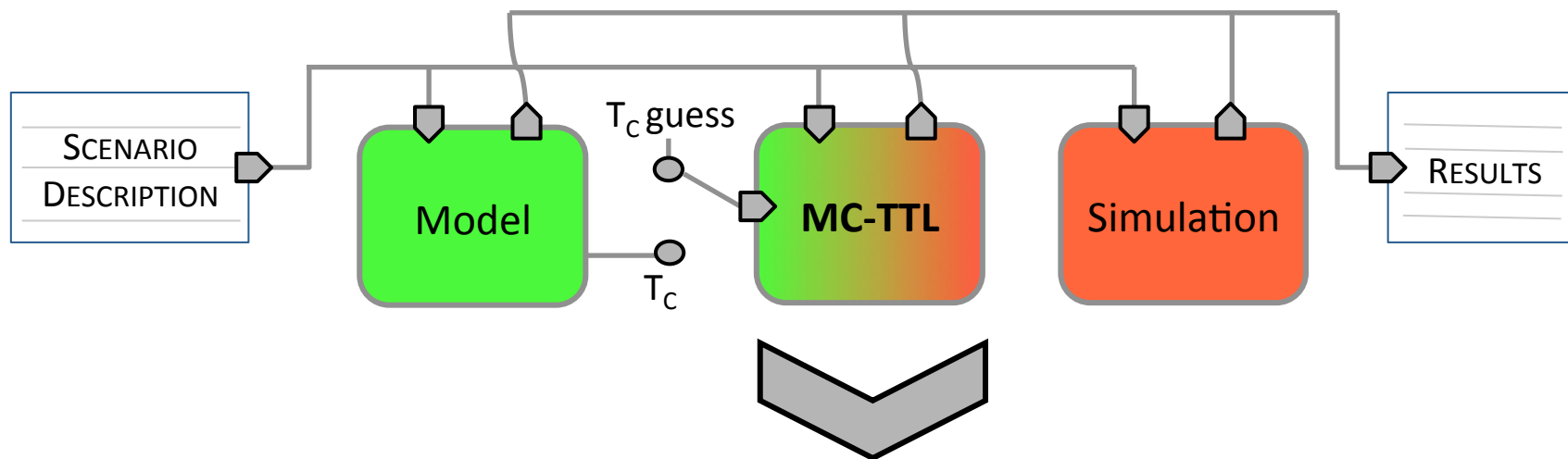
Assumed to be **CONSTANT**, independent from the content

- $p_{in}(\lambda_m, T_C) = 1 - e^{-\lambda_m T_C}$

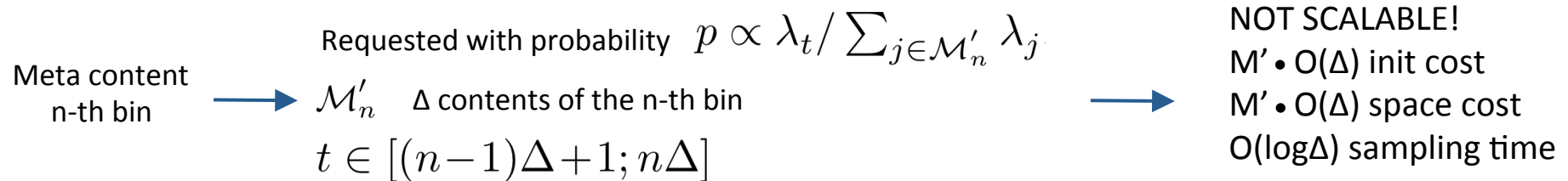
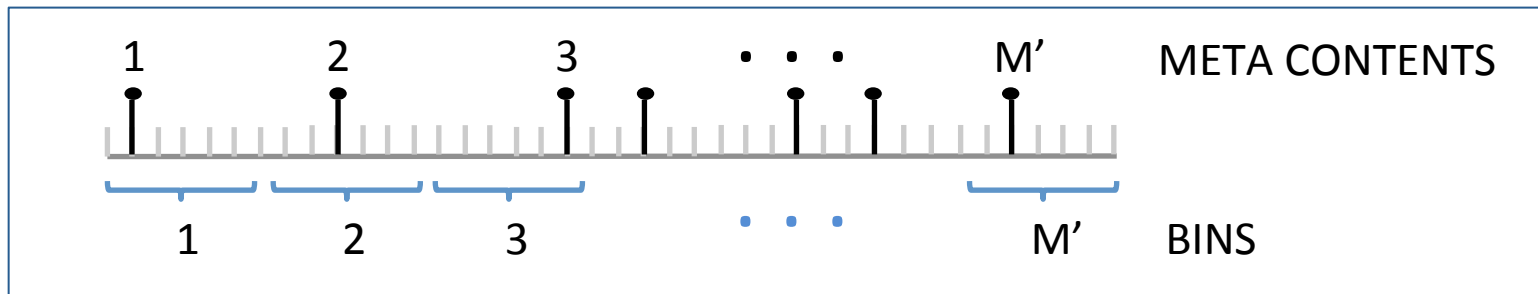
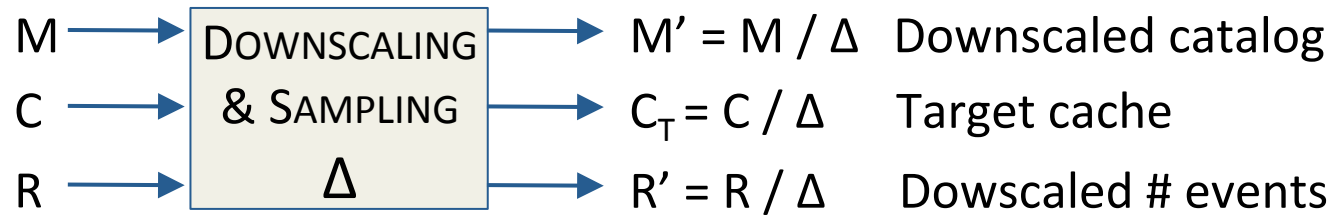
- $C = \mathbb{E}[C] = \mathbb{E} \sum_m [1_{\{m \text{ in cache at } t\}}] = \sum_m p_{in}(\lambda_m, T_C)$

- $p_{hit} = \sum_m \lambda_m p_{in}(\lambda_m, T_C) / \sum_m \lambda_m$

# UNDER THE HOOD



# DOWNSCALING & SAMPLING



## Rejection Inversion Sampling (VERY SCALABLE!)

Extract Zipf's distributed random numbers between  $[1, \Delta]$   
 No Memory and  $O(1)$  runtime complexity



# STABILITY CHECK

Pivotal role to simulate the  $R'^{(1)}$  requests at steady state

Dynamic transient period  
(routing, meta-caching, topology,...)  $\longrightarrow$  **Adaptive Stability Monitor**

- Coefficient of Variation (**CV**) of the mean hit probability (  $CV = \text{std}(p_{\text{hit}}) / E(p_{\text{hit}})$  )
- Batch mean of  $W$  samples (new sample iif active cache and state change)
- Check stability (i.e.,  $CV < 5 \cdot 10^{-3}$ ) for the first  $\mathbf{N}' = \mathbf{Y} \cdot \mathbf{N}$  nodes, where  $\mathbf{Y} \in ]0,1]$ .

(1)

ED-Sim:  $\text{end} = R / (\Lambda \cdot Cl)$ , with  $\Lambda = \sum_{i \in M} \lambda_i$

MC-TTL:  $\text{end}' = R' / (\Lambda' \cdot Cl)$ , with  $\Lambda' = \sum_{j \in M'} \lambda_i \approx \Lambda / \Delta$

Since  $\text{end} = \text{end}' \rightarrow R' = R / \Delta$

# $T_C$ CORRECTION & CONSISTENCY CHECK

**Hp:** each TTL cache will store, on average,  $C_T = C/\Delta$  contents at steady state if its *eviction time* corresponds to the *characteristic time*  $T_C$  of its equivalent LRU non-scaled cache.

**Controlled Variable** = Measured Cache Size  $C_M$

$$C_{M_i}(k+1) = \frac{C_{M_i}(k) t(k) + B_i(k+1) [t(k+1) - t(k)]}{t(k+1)}$$

$C_{M_i}(k+1)$  = online avg of the cache size of the  $i$ -th node @  $k$ -th measurement time

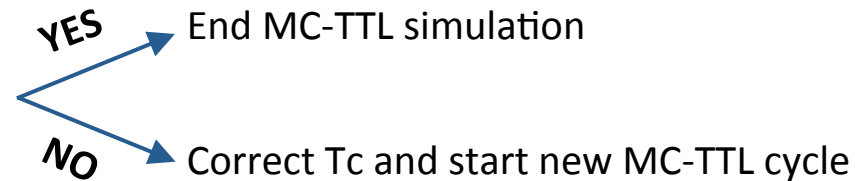
$B_i(k+1)$  = actual # contents stored inside the TTL cache

Samples are taken every miss event with probability  $p=0.1$

**Consistency Check** (after  $R'$  events)

$$\frac{1}{N'} \sum_{i \in N'} \frac{|C_T - C_{M_i}|}{C_T} < 0.1$$

Same  $N'$  nodes  
(coherent with stability check)



$$T_{C_i}(z+1) = T_{C_i}(z) \left( \frac{C_T}{C_{M_i}(z)} \right)$$

$C_M$  distance from  $C_T$  connected to input  $T_C$   
distance from real  $T_C$  (the higher  $T_C$  the bigger  $C_M$ )

# T<sub>C</sub> SENSITIVITY - I

## 4-level Binary Tree

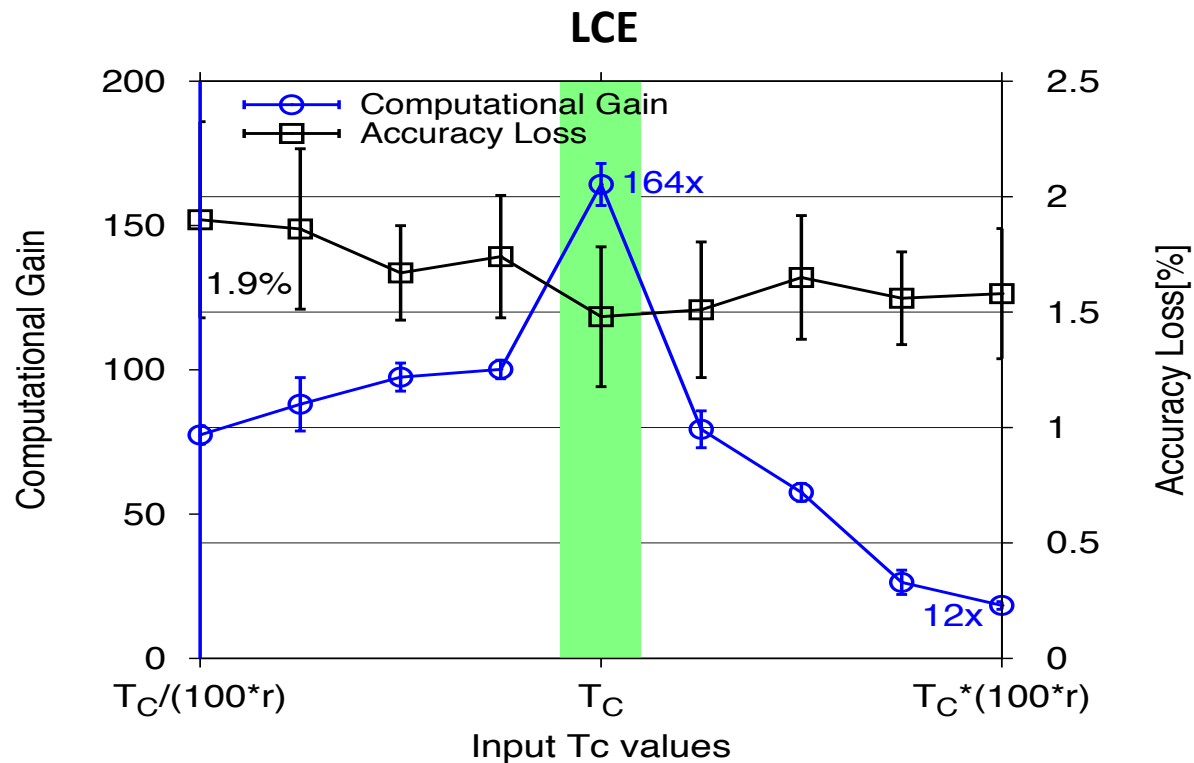
| Cache | - C = 1e3  
 | Catalog | - M = 1e6      Downscaling Factor - Δ = 1e2  
 # Requests - R = 1e7

Level	Tc Values [s]			
	LCE	FIX0.1	LCD	2-LRU (Name/Main)
0 (Root)	11	115	13	14 / 654
1	22	218	1090	27 / 1040
2	43	400	1250	51 / 1420
3 (Leaves)	75	570	815	75 / 1255
P_hit @ Stab.	22.8	25.9	28.5	29.2
P_hit @ End.	22.8	26.3	28.1	29.4
Stab. Time	8.4	10.3	14.4	23.7
End Time	482.7	390	386	456.3

# $T_C$ SENSITIVITY - II

## 4-level Binary Tree

| Cache | - C = 1e5  
 | Catalog | - M = 1e8      Downscaling Factor -  $\Delta = 1e4$   
 # Requests - R = 1e8



**Simulation:** Phit = 30.6% - CPU = 4089 s - Mem = 673 MB  
**Model:** Phit = 29.8% - CPU = 740 s - Mem = 24240 MB  
**MC-TTL:** - Mem  $\approx$  38 MB (18x)

# YOTTA SENSITIVITY

## NDN Testbed

| Cache | - C = 1e3  
 | Catalog | - M = 1e6      Downscaling Factor - Δ = 1e3  
 # Requests - R = 1e7

Sim. Type	Yotta	P_hit @ Stab.	P_hit @ End	Stab. Time [s]	End Time [s]
<b>ED-Sim</b>	1	33.8	33.9	99.7	458.0
	0.95	33.7	33.9	42.4	432.5
	0.9	33.7	33.9	35.0	421.9
	0.75	33.6	33.9	29.3	408.13
	0.5	32.8	33.9	15.4	401.33